

Probabilistic Logic Programming with Fusemate: Main Ideas and Recent Developments

Peter Baumgartner

CSIRO/Data61 (StatML)
ANU CECC

About

- PhD in 1996 in Germany, on Automated Reasoning
- NICTA 2005, CSIRO since 2014

Research Interest

Knowledge representation and reasoning

Designing inference systems

Applications

Recently

Probabilitistic Logic Programming (PLP)

Combination with LLM (with Lachlan McGinness)

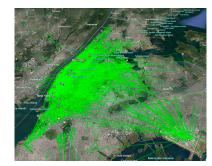
D61 Applications



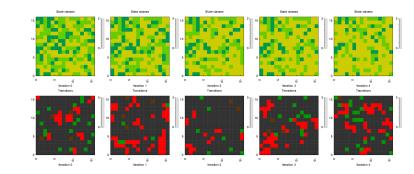


Factory floor

Computer Factory



Taxi rides in NYC



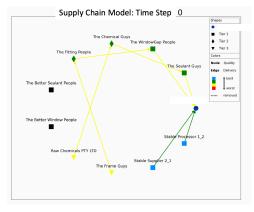
Valuing Sustainability - Future states





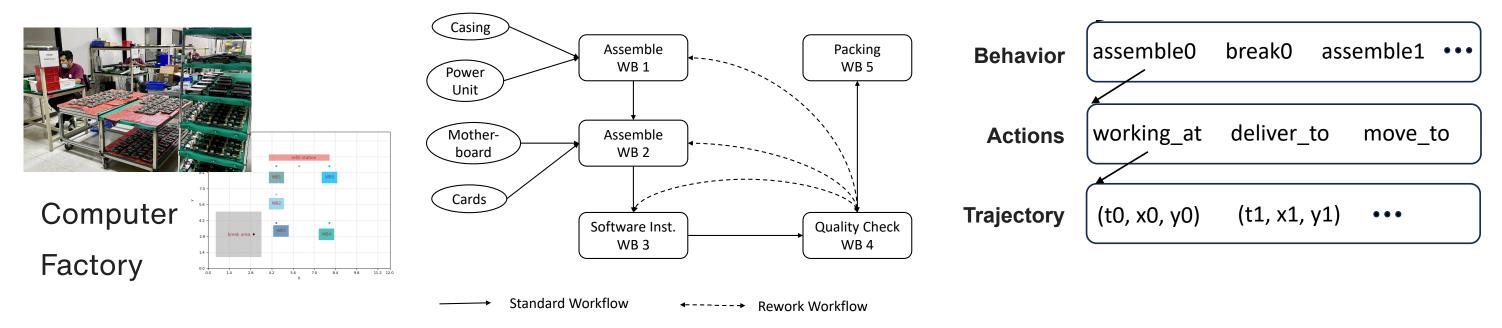


Beef supply chain

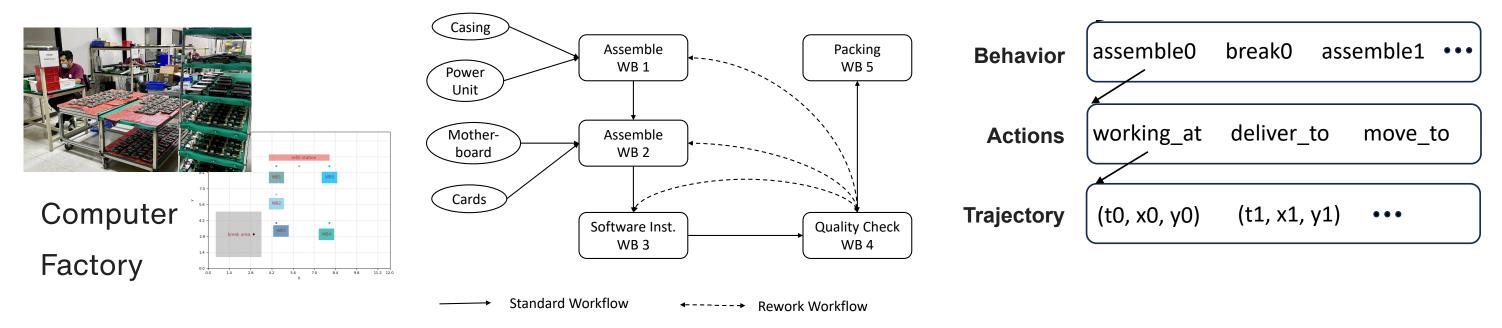


Factory supply chain

States - Transitions - Uncertainty

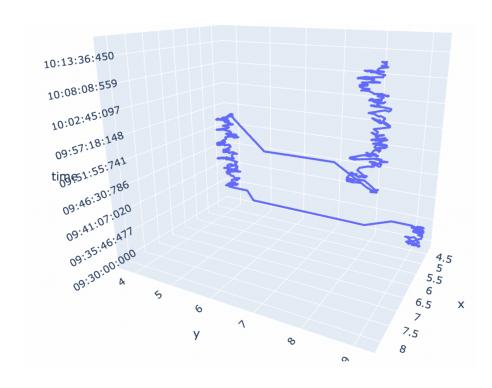


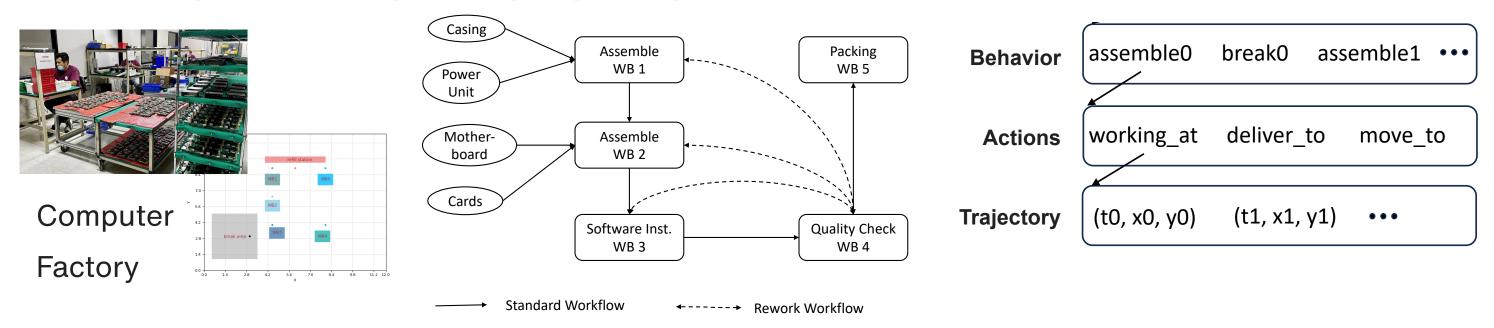
Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory





Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory



Probabilistic logic program

```
10:13:36:450

10:08:08:559

10:02:45:097

09:57:18:148

tigges1:55:741

09:46:30:786

09:41:07:020

09:41:07:020

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:35:46:477

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

09:36:47*

00:36:47*

00:36:47*

00:36:47*

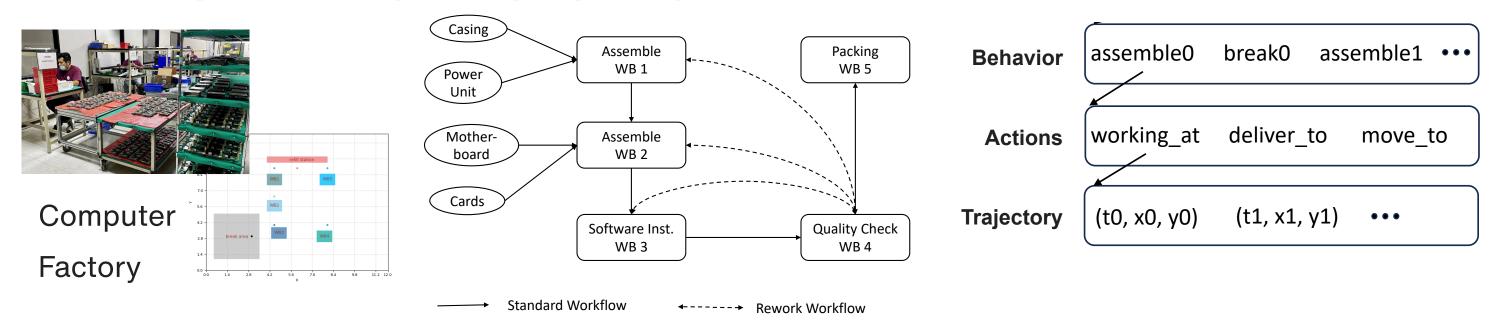
00:36:47*

00:36:47*

00:36:47*

00:36:47*

00:
```



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory



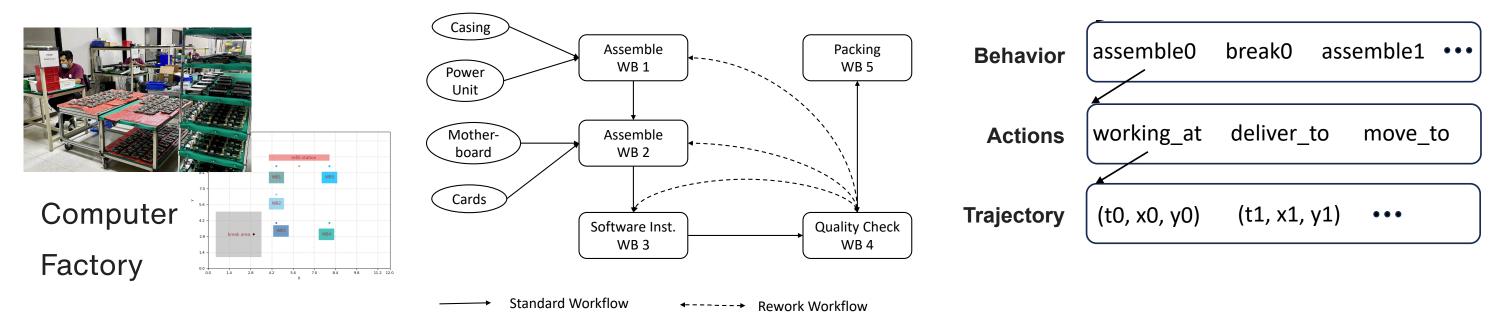
10:13:36:450 10:08:08:559 10:02:45:097 09:57:18:148 tigges1:55:741 09:46:30:786 09:41:07:020 09:35:46:477

Probabilistic logic program



Most likely behaviour seq.

```
behaviour ~ [assemble, break ...]. %% Distribution
worker \sim [1,2,3,4,5].
                                    %% Distribution
action = working_at(wb(W))
                             @ 0 :-
    behaviour = assemble,
    worker = W.
action = deliver_to(wb(W+1)) @ 1 :-
    behaviour = assemble,
    worker = W.
              @ T :- action = working_at(L) @ T.
dur ~ [1..10] @ T :- action = working_at(_) @ T.
```



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory

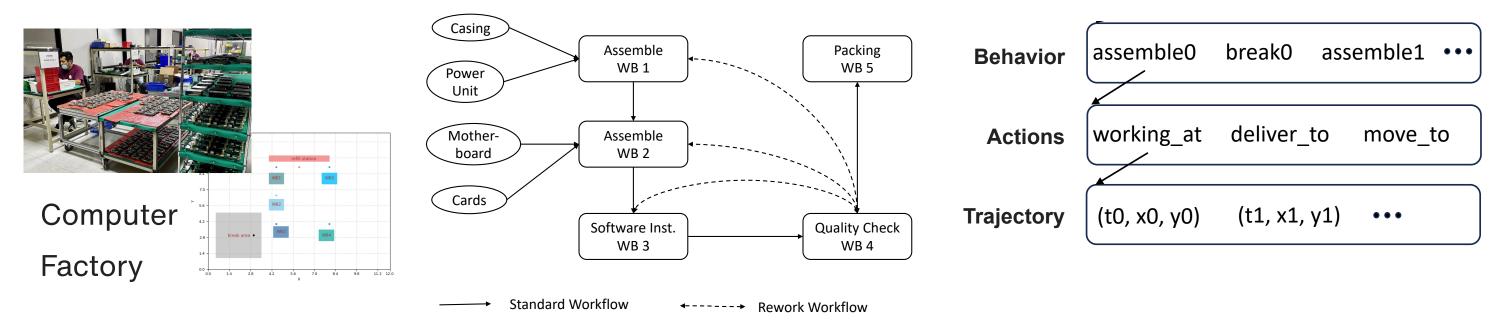


10:13:36:450 10:08:08:559 10:02:45:097 09:57:18:148 tiggs:1:55:741 tiggs:1:55:741 09:46:30:786 09:46:407 09:35:46:477 09:35:46:477 09:35:46:477 09:30:00 09:30:00 4.5 5.5 6.5 X

Probabilistic logic program



Most likely behaviour seq.



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory

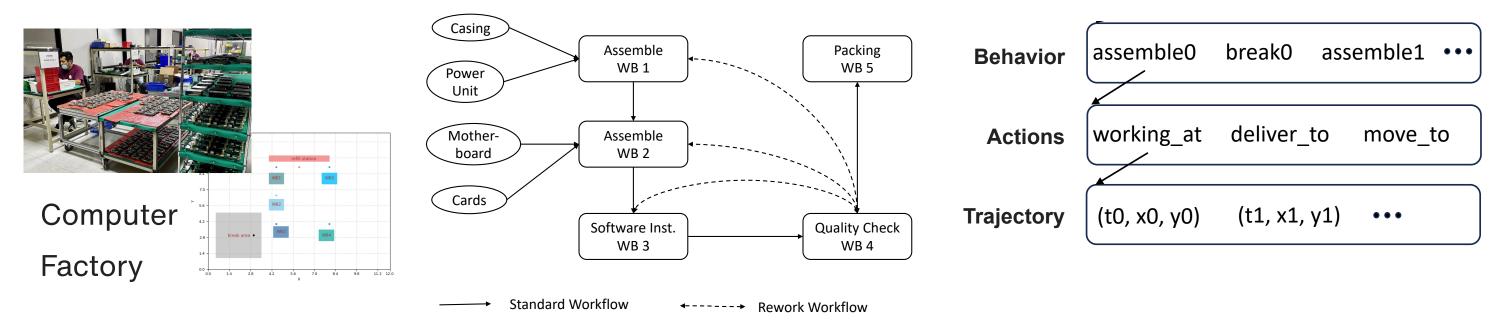


10:13:36:450 10:08:08:559 10:02:45:097 09:57:18:148 tigges1:55:741 tigges1:55:741 09:36:46:30:786 09:46:30:786 09:35:46:477 09:36:46:477 09:36:46:477 09:36:46:477 09:36:46:477 09:36:46:477

Probabilistic logic program



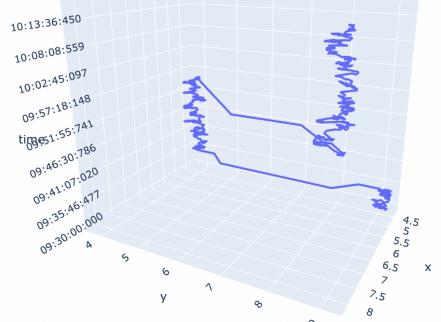
Most likely behaviour seq.



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory



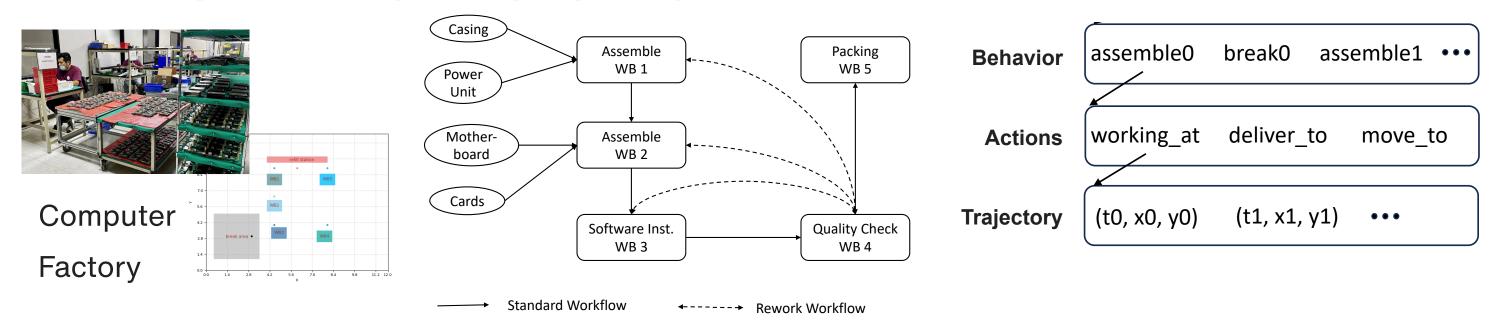


Probabilistic logic program



```
behaviour ~ [assemble, break ...].
                                    %% Distribution
worker \sim [1,2,3,4,5].
                                     %% Distribution
action = working_at(wb(W))
                              'a 0
    behaviour = assemble,
    worker = W.
action = deliver_to(wb(W+1)) @ 1
    behaviour = assemble,
    worker = W.
                     action = working_at(L) @ T.
loc = L
                     action = working_at(_) @ T.
```

Most likely behaviour seq.



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory



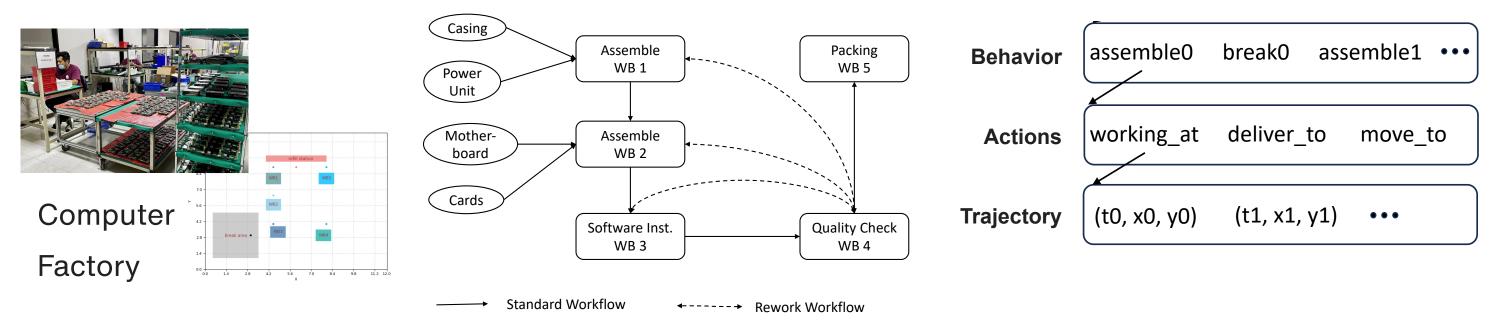
10:13:36:450 10:08:08:559 10:02:45:097 09:57:18:148 tigges1:55:741 tigges1:55:741 09:36:46:30:786 09:46:30:786 09:35:46:477 09:36:46:477 09:36:46:477 09:36:46:477 09:36:46:477 09:36:46:477

Probabilistic logic program



Most likely behaviour seq.

```
behaviour ~ [assemble, break ...].
                                   %% Distribution
worker \sim [1,2,3,4,5].
                                   %% Distribution
action = working_at(wb(W))
                            'a 0
    behaviour = assemble,
    worker = W.
                                                 Hidden Markov Model
action = deliver_to(wb(W+1)) @ 1
    behaviour = assemble,
   worker = W.
                    action = working_at(L) @ T.
loc = L
                    action = working_at(_) @ T.
dur ~ [1..10] @ T :
```



Problem: Trajectory classification: what actions/behaviours exhibited by a trajectory?

Given trajectory



10:13:36:450 10:08:08:559 10:02:45:097 09:57:18:148 tiggs:1:55:741 tiggs:1:7:020 09:41:07:020 09:30:00 09:30:00 4.5 5.5 6.5 7 7 8

Probabilistic logic program



Most likely behaviour seq.

assemble -> break -> ...

loc = L @ T action = working_at(L) @ T.
dur ~ [1..10] @ T : action = working_at(_) @ T.

Probabilistic

Part 1

- Logic
- Programming
- Fusemate Implementation

Part 2

- LLMs + Logic (Programming)
- Neural Networks + Logic (Programming

"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution

Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

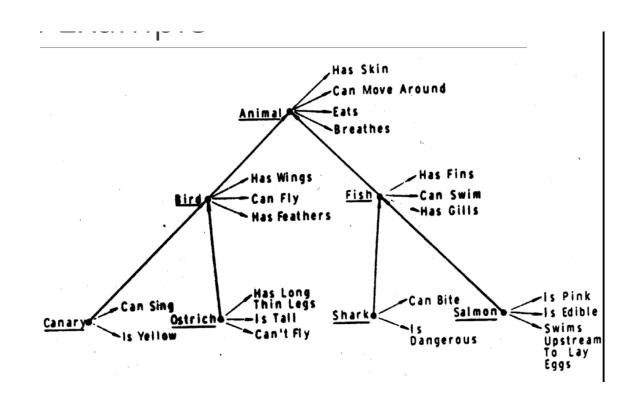
Query answering

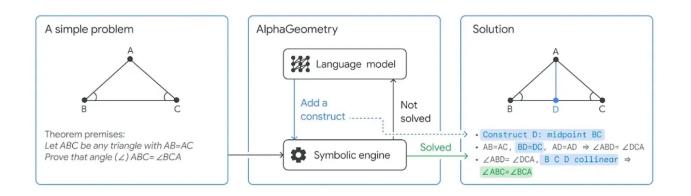
Model computation

Knowledge Completion

Diagnosis

$$\begin{split} & \text{flight(toronto, london)}. \\ & \text{flight(london, rome)}. \\ & \text{flight(chicago, london)}. \\ & \text{flight}(X,Y) \coloneq \text{flight}(X,Z) \text{ , flight}(Z,Y). \end{split}$$





AlphaGeometry, AlphaProof, LLM-modulo, ...

"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution

Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

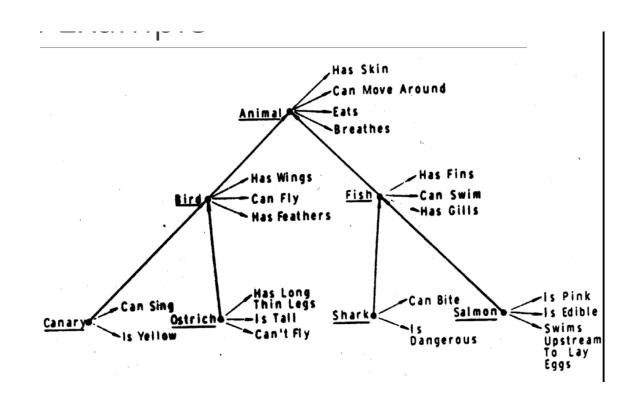
Query answering

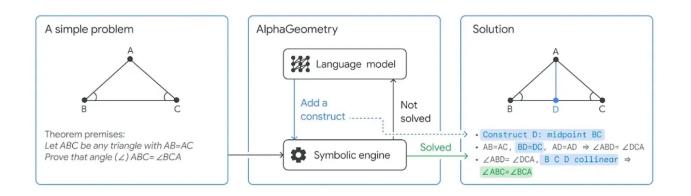
Model computation

Knowledge Completion

Diagnosis

$$\begin{split} & \text{flight(toronto, london)}. \\ & \text{flight(london, rome)}. \\ & \text{flight(chicago, london)}. \\ & \text{flight}(X,Y) \coloneq \text{flight}(X,Z) \text{ , flight}(Z,Y). \end{split}$$





AlphaGeometry, AlphaProof, LLM-modulo, ...

"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution

Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

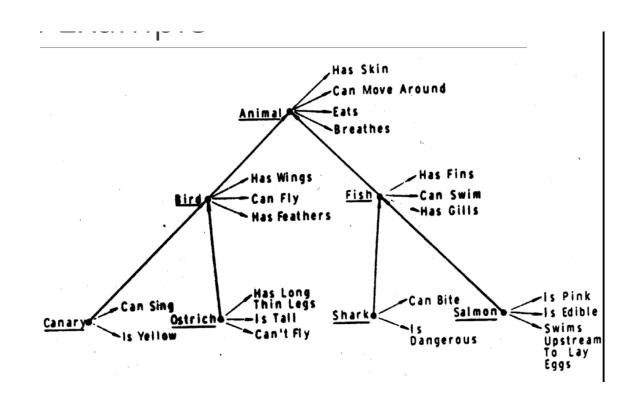
Query answering

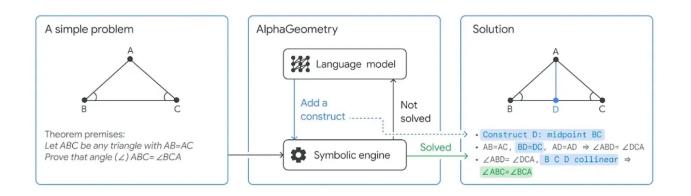
Model computation

Knowledge Completion

Diagnosis

$$\begin{split} & \text{flight(toronto, london)}. \\ & \text{flight(london, rome)}. \\ & \text{flight(chicago, london)}. \\ & \text{flight}(X,Y) \coloneq \text{flight}(X,Z) \text{ , flight}(Z,Y). \end{split}$$





AlphaGeometry, AlphaProof, LLM-modulo, ...

"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution



Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

Query answering

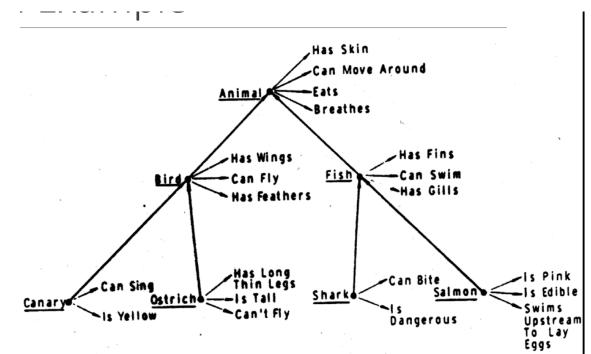
Model computation

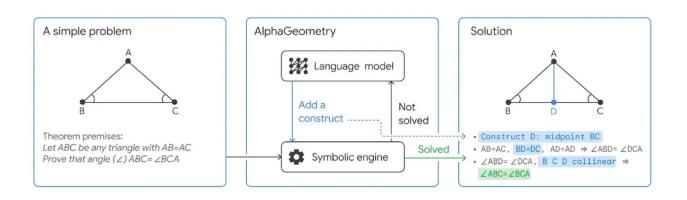
Knowledge Completion

Diagnosis

flight(london, rome).
flight(chicago, london).
flight(X, Y) :- flight(X, Z), flight(X, Y).

flight(toronto, london).





"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution



Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

Query answering

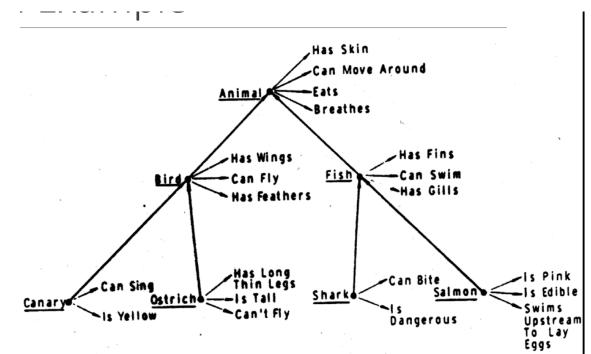
Model computation

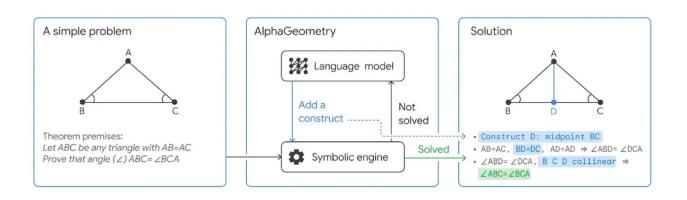
Knowledge Completion

Diagnosis

flight(london, rome).
flight(chicago, london).
flight(X, Y) :- flight(X, Z), flight(X, Y).

flight(toronto, london).





"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution



Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

Query answering

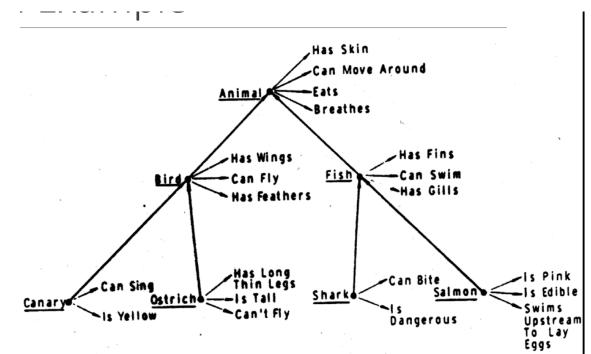
Model computation

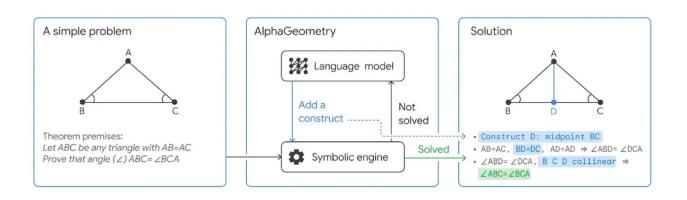
Knowledge Completion

Diagnosis

flight(london, rome).
flight(chicago, london).
flight(X, Y) :- flight(X, Z), flight(X, Y).

flight(toronto, london).





"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution



Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

Query answering

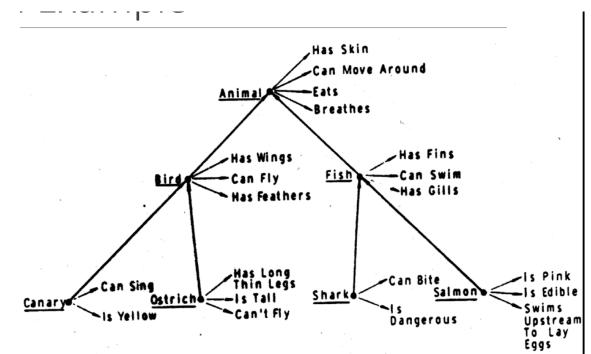
Model computation

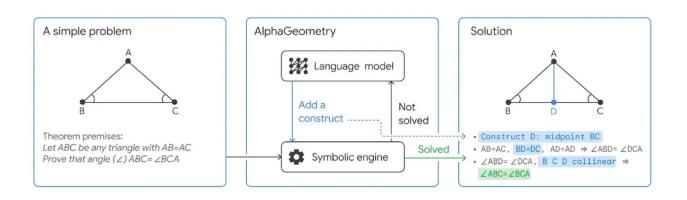
Knowledge Completion

Diagnosis

flight(london, rome).
flight(chicago, london).
flight(X, Y) :- flight(X, Z), flight(X, Y).

flight(toronto, london).





"Algorithm = Logic + Control"

- Model the problem at hand with "logic"
- Feed into automated reasoning system
- Push button and get solution



Logic

Classical

Non-monotonic

Modal

Probabilistic

Temporal

Graphs (Ontologies)

Relational (Tables)

Built-in Theories

Reasoning Tasks

Proving

Disproving

Query answering

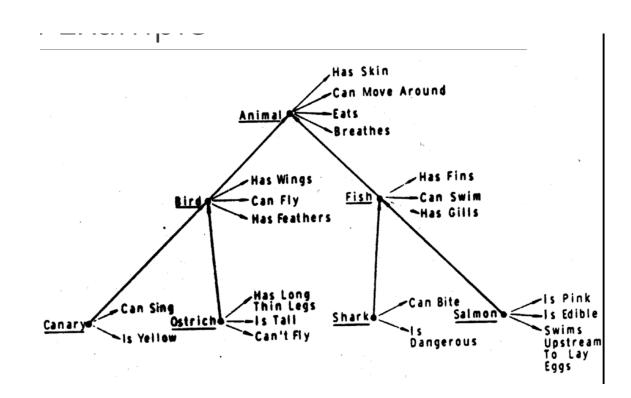
Model computation

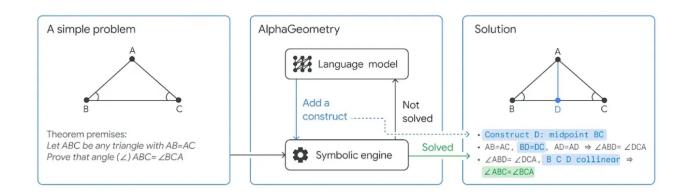
Knowledge Completion

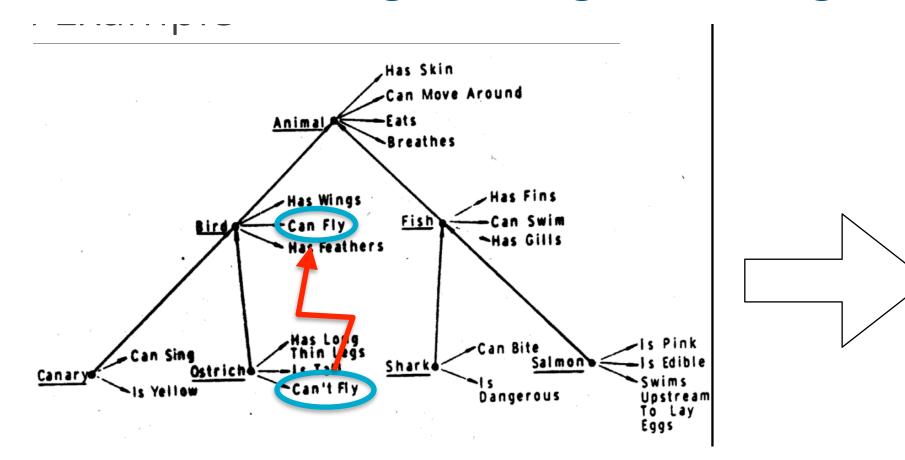
Diagnosis

"Logic" vs "Logic Programming"?

$$\begin{split} & \text{flight}(\text{toronto}, \text{london}). \\ & \text{flight}(\text{london}, \text{rome}). \\ & \text{flight}(\text{chicago}, \text{london}). \\ & \text{flight}(X, Y) \coloneq \text{flight}(X, Z) \text{ , flight}(Z, Y). \end{split}$$



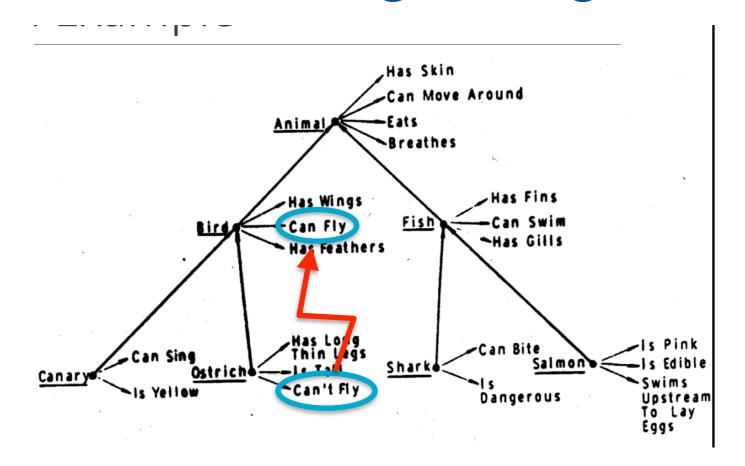


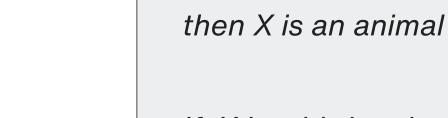


If X is a bird then X is an animal

If X is a bird and
X is **not** an ostrich
then X can fly

Tweety is a bird (Tweety is an ostrich)





If X is a bird

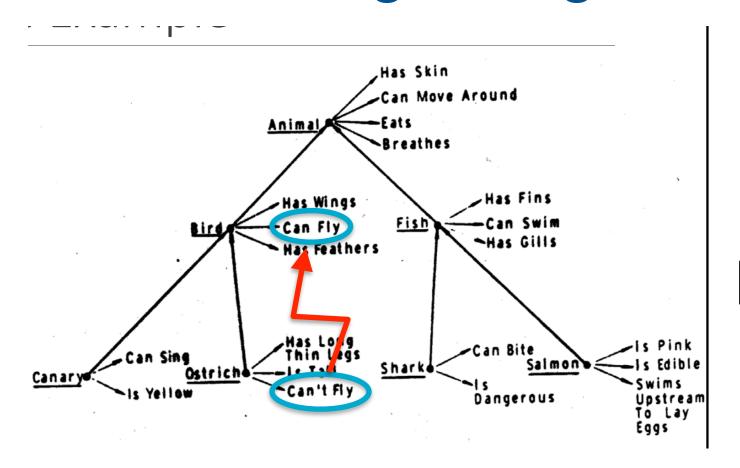
If X is a bird and
X is **not** an ostrich
then X can fly

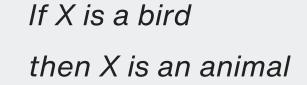
Tweety is a bird (Tweety is an ostrich)

Classical (Open-World) Entailment

Non-Monotonic (Closed-World)

"Constraint" view





If X is a bird and
X is **not** an ostrich
then X can fly

Tweety is a bird (Tweety is an ostrich)

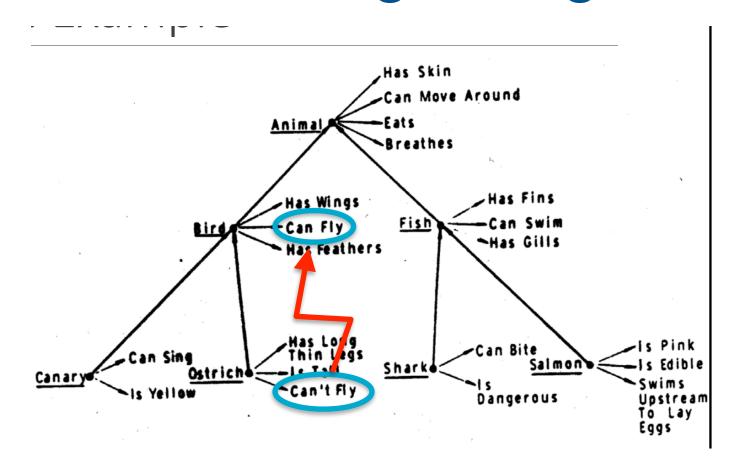
Classical (Open-World) Entailment

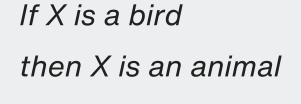
✓ Tweety is an animal

Non-Monotonic (Closed-World)

Tweety is an animal

"Constraint" view





If X is a bird and
X is **not** an ostrich
then X can fly

Tweety is a bird (Tweety is an ostrich)

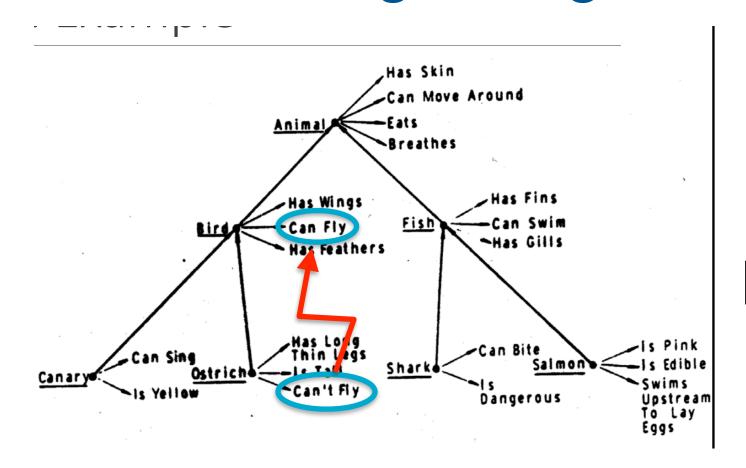
Classical (Open-World) Entailment

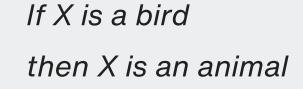
- ✓ Tweety is an animal
- X Tweety can fly

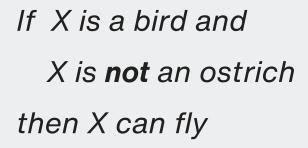
"Constraint" view

Non-Monotonic (Closed-World)

- ✓ Tweety is an animal
- Tweety can fly







Tweety is a bird (Tweety is an ostrich)

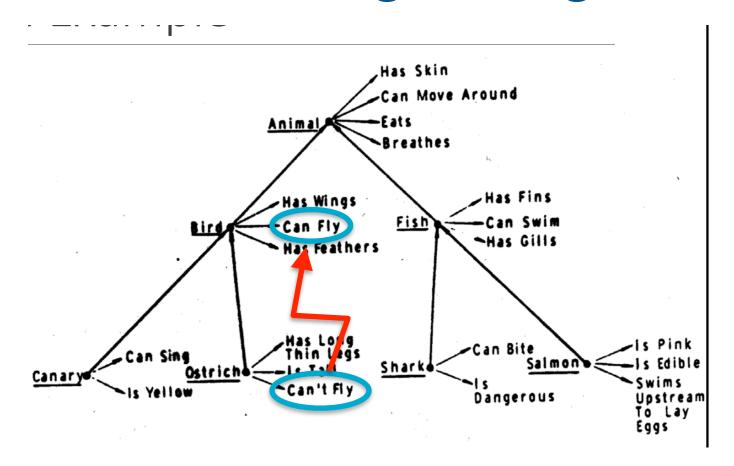
Classical (Open-World) Entailment

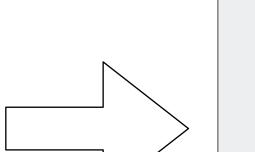
- Tweety is an animal
- X Tweety can fly
- X Tweety cannot fly

"Constraint" view

Non-Monotonic (Closed-World)

- Tweety is an animal
- Tweety can fly
- X Tweety cannot fly





If X is a bird then X is an animal

If X is a bird and
X is **not** an ostrich
then X can fly

Tweety is a bird (Tweety is an ostrich)

Classical (Open-World) Entailment

- Tweety is an animal
- X Tweety can fly
- X Tweety cannot fly

"Constraint" view

Non-Monotonic (Closed-World)

- Tweety is an animal
- ✓ Tweety can fly
- Tweety cannot fly



Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Facts Rules	cat(tom). drinks(X, milk) :- cat(X).	
Default Negation	innocent(X) := cat(X), not	guilty(X).
	flies(X) :- bird(X), not abn	ormal(X).
@ Time	thirsty(X) @ T+1:-	
(Fusemate)	thirsty(X) @ T,	
	not drink(X, _) @ T.	
Probabilities	0.8 :: cat(tom).	
	0.5 :: drinks(X, milk) :- cat	t(X).
Distributions	nr_siblings(X) ~ [[0, 0.05],	[1, 0.10], [5, 0.10]]
(Fusemate)	:- cat(X).	
	?- thirsty(tom) @ T	
Queries	thirsty(tom) @ 2, dri	nk(tom, milk) @ 5.



Tom is a cat If X is a cat then X drinks milk

If X is a cat and X is not guilty

If X is thirsty at time T and X does not drink at time T then X is thirsty at time T+1

then X is innocent

Operational

Dynamic Data Structures and Distributions

Drawing without replacement

 $\% \ 0.5 :: \ \lceil C1 = \text{green}, \ C2 = \text{red} \rceil$

```
urn([r(1), r(2), g(1)]) @ 0.
                                      %% Initially two red and one green distinguishable balls
draw ~ Balls @ T :-
                                      %% Draw a ball uniformly if urn is not empty
   urn(Balls) @ T,
   Balls \= [].
urn(Balls -- [B]) @ T+1 :-
                                      %% Drawing a ball removes it from urn
   urn(Balls) @ T,
    draw = B @ T.
some(green) @ T :- draw=g(\underline{\ }) @ T.
Queries
?- some(green) @ 0.
% 0.333333
?- some(green) @ 1 | some(red) @ 0.
% 0.5 conditional query
?- some(C1) @ 1, some(C2) @ 2 | some(red) @ 0. % Non-ground conditional query, two solutions:
\% 0.5 :: [C1 = red, C2 = green]
```

Dynamic Data Structures and Distributions

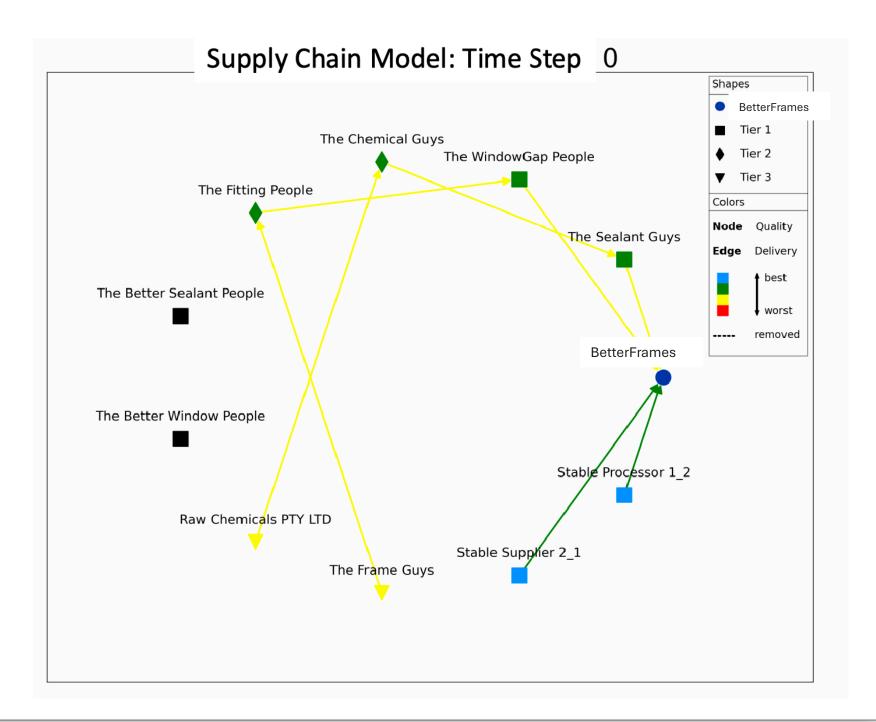
Drawing without replacement

```
urn([r(1), r(2), g(1)]) @ 0.
draw ~ Balls @ T :-
    urn(Balls) @ T,
    Balls \= [].
urn(Balls -- [B]) @ T+1 :-
    urn(Balls) @ T,
    draw = B @ T.
some(red) @ T :- draw=r(_) @ T.
some(green) @ T :- draw=g(_) @ T.
```

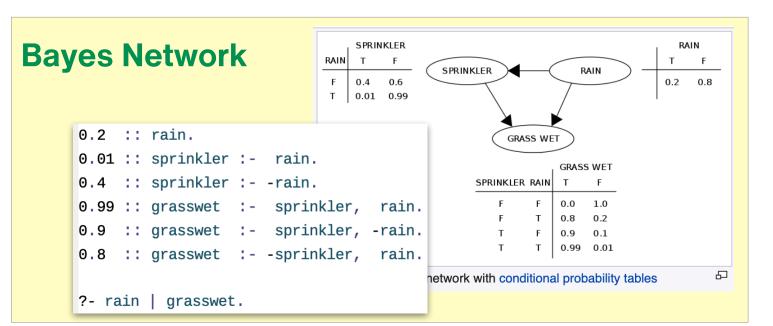
Queries

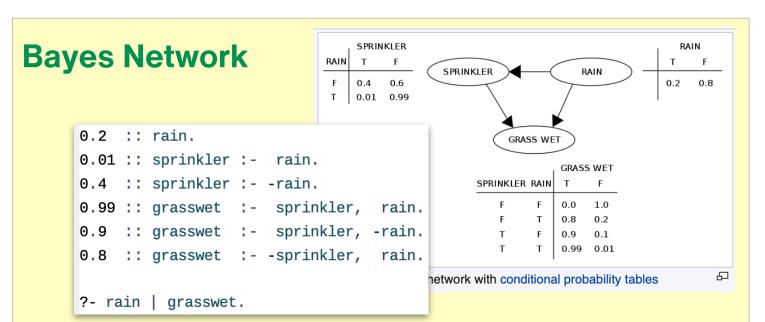
```
?- some(green) @ 0.
% 0.333333
?- some(green) @ 1 | some(red) @ 0.
% 0.5 conditional query
?- some(C1) @ 1, some(C2) @ 2 | some(red)
% 0.5 :: [C1 = red, C2 = green]
% 0.5 :: [C1 = green, C2 = red]
```

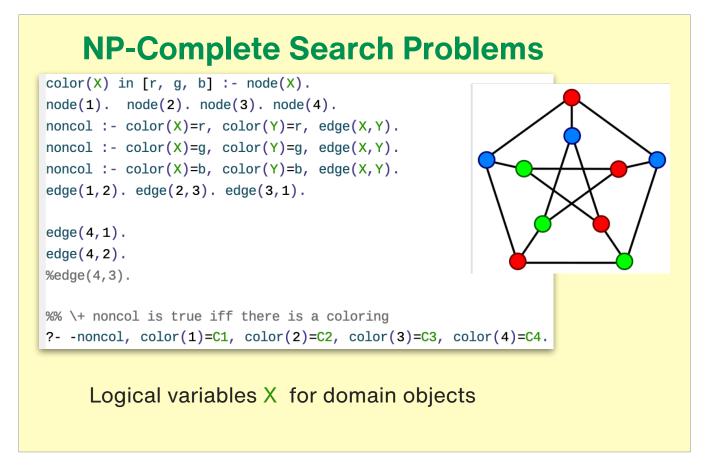
D61 Supply Chain Risk Assessment Application



Probabilistic Logic Programming (Fusemate)



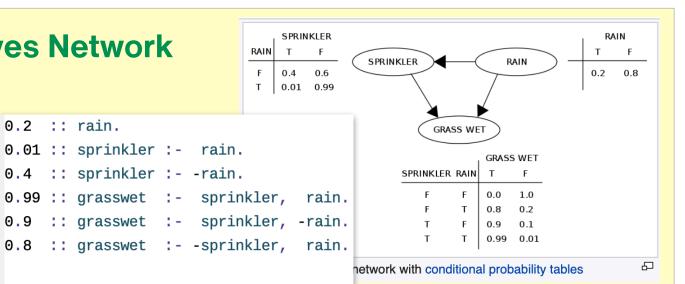




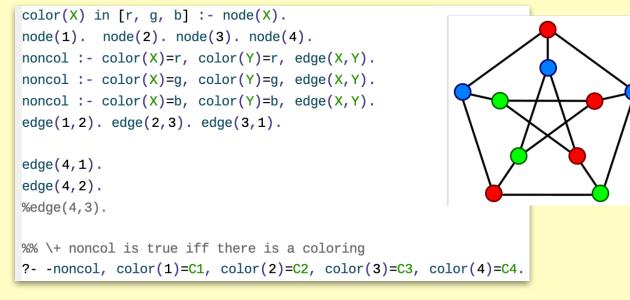
Bayes Network

0.2 :: rain.

?- rain | grasswet.



NP-Complete Search Problems



Logical variables X for domain objects

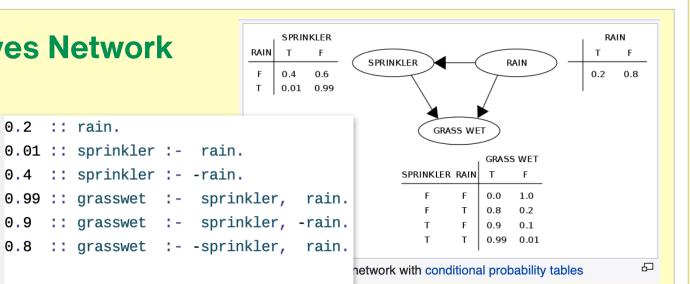
Time

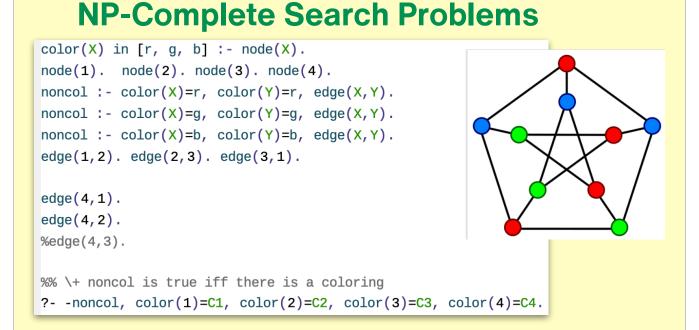
```
%% Some "random" blockag
block(1) @ 2.
block(2) @ 3.
prob(0).
(0.5 :: prob(K+1) + prob(K)) @ N+1 :-
    prob(K) @ N,
    \+ bl(K) @ N.
                     %% ?- prob(K) @ 4.
prob(K) @ N+1 :-
                     0.0625 :: prob(0) @ 4
    prob(K) @ N,
                     0.3750 :: prob(1) @ 4
                     0.43750 :: prob(2) @ 4
    bl(K) @ N.
                     0.0625 :: prob(3) @ 4
                     0.0625 :: prob(4) @ 4
```

Bayes Network

0.2 :: rain.

?- rain | grasswet.

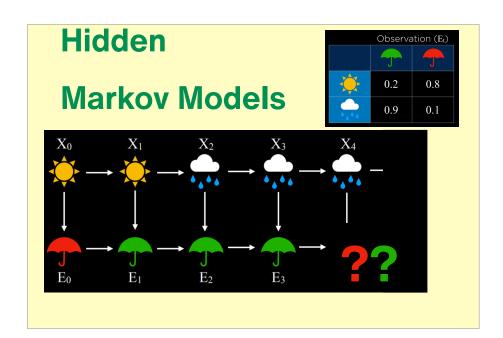




Logical variables X for domain objects

Time

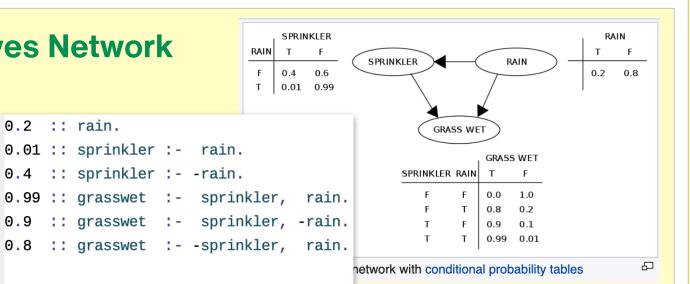
```
%% Some "random" blockag
block(1) @ 2.
block(2) @ 3.
prob(0).
(0.5 :: prob(K+1) + prob(K)) @ N+1 :-
    prob(K) @ N,
    \+ bl(K) @ N.
                     %% ?- prob(K) @ 4.
prob(K) @ N+1 :-
                     0.0625 :: prob(0) @ 4
    prob(K) @ N,
                     0.3750 :: prob(1) @ 4
                     0.43750 :: prob(2) @ 4
    bl(K) @ N.
                     0.0625 :: prob(3) @ 4
                     0.0625 :: prob(4) @ 4
```



Bayes Network

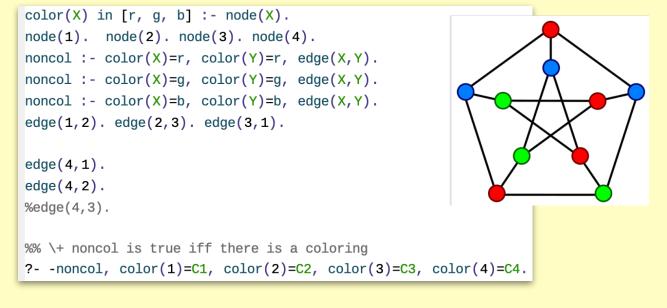
0.2 :: rain.

?- rain | grasswet.



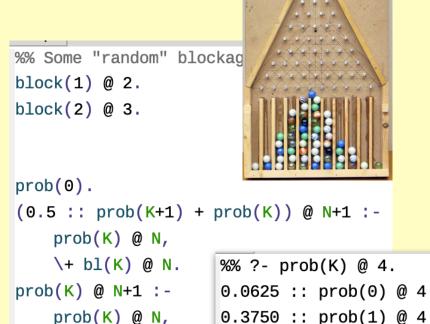
NP-Complete Search Problems

Logical variables X for domain objects



Time

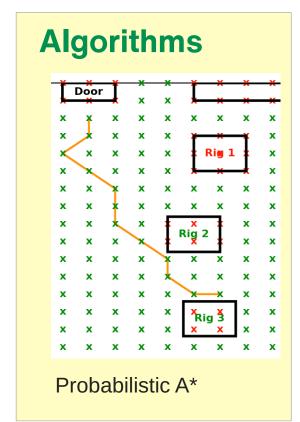
bl(K) @ N.

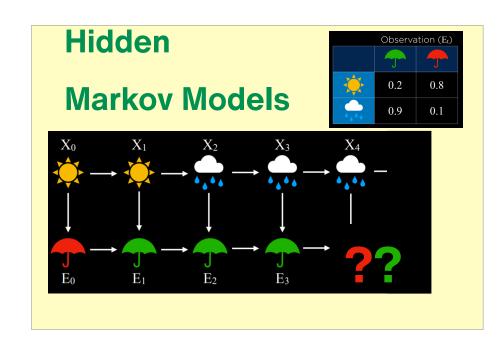


0.43750 :: prob(2) @ 4

0.0625 :: prob(3) @ 4

0.0625 :: prob(4) @ 4

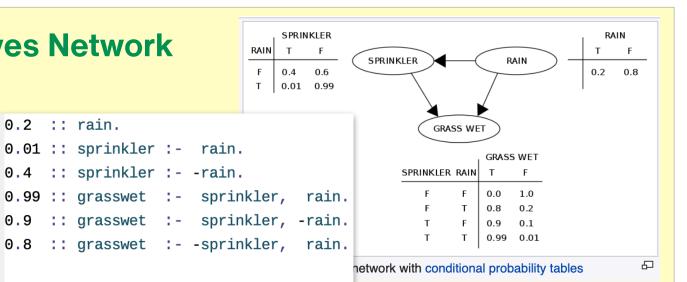




Bayes Network

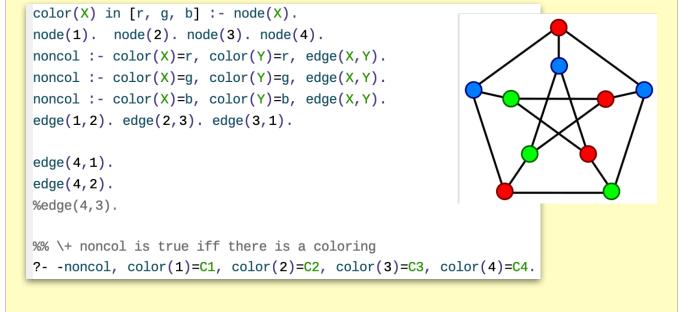
0.2 :: rain.

?- rain | grasswet.

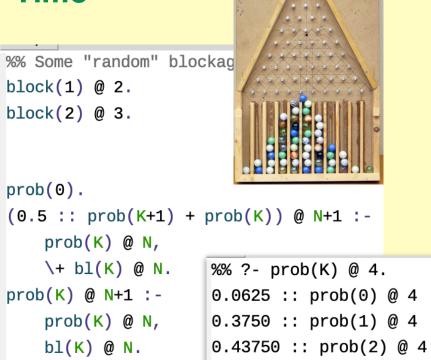


NP-Complete Search Problems

Logical variables X for domain objects

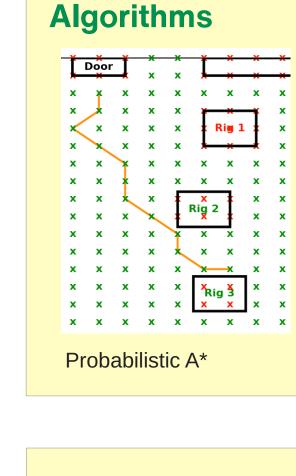


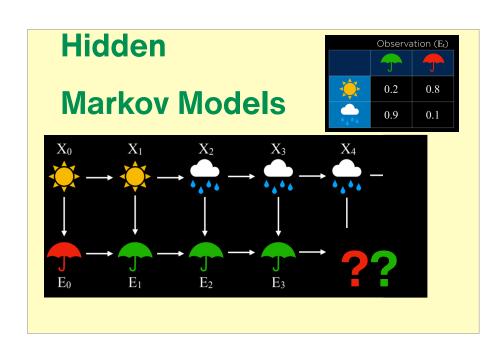
Time

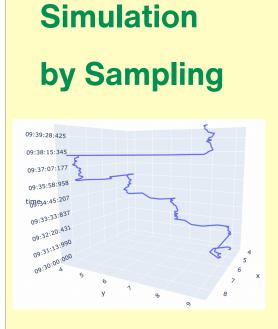


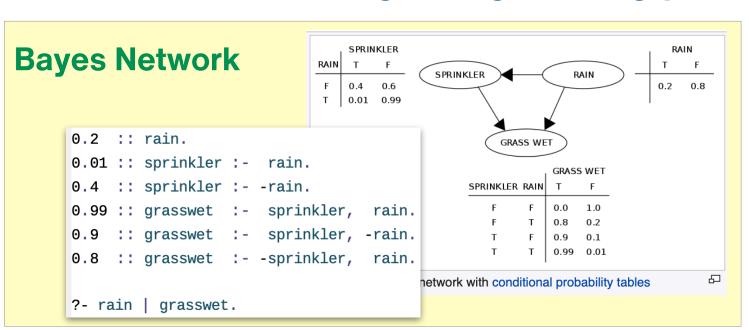
0.0625 :: prob(3) @ 4

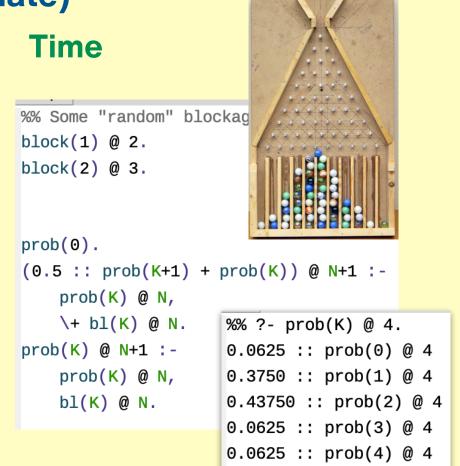
0.0625 :: prob(4) @ 4

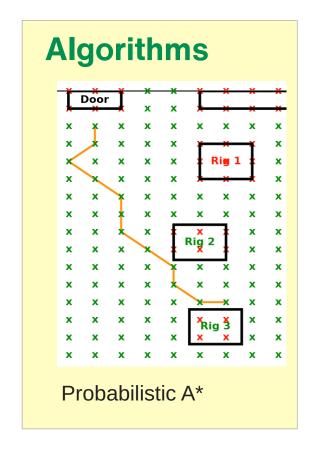


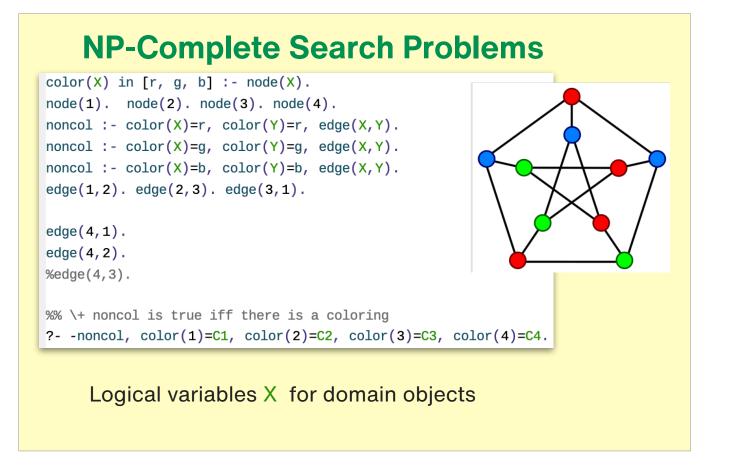


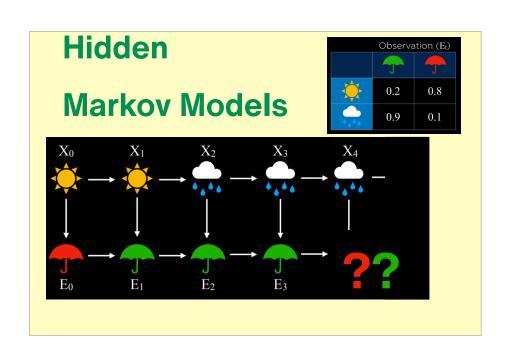


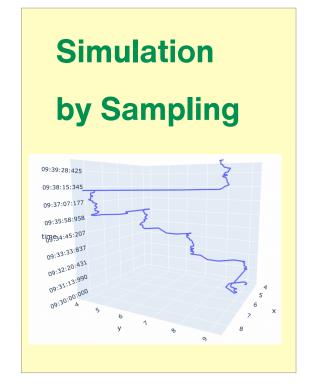












Fusemate Probabilistic Logic Programming System

Implementation in Python

(From earlier versions in Scala)

Two-way interface Python <-> Fusemate

Python data structures available in Fusemate

Logic program can be written as Python functions

Efficient probablistic inference

Default negation via well-founded model

Rules cannot change past states

Two-phase inference algorithm

Phase 1 "grounding"

Removal of first-order variables

- -> Bayes-net like program (may contain cycles)
- Pase 2 inference/sampling

Top-down variable elimination with caching of results

Strong Python integration

Fusemate Probabilistic Logic Programming System

Implementation in Python

(From earlier versions in Scala)

Two-way interface Python <-> Fusemate

Python data structures available in Fusemate

Logic program can be written as Python functions

Efficient probablistic inference

Default negation via well-founded model

Rules cannot change past states

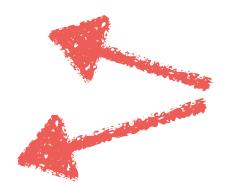
Two-phase inference algorithm

Phase 1 "grounding"
 Removal of first-order variables

- -> Bayes-net like program (may contain cycles)
- Pase 2 inference/sampling

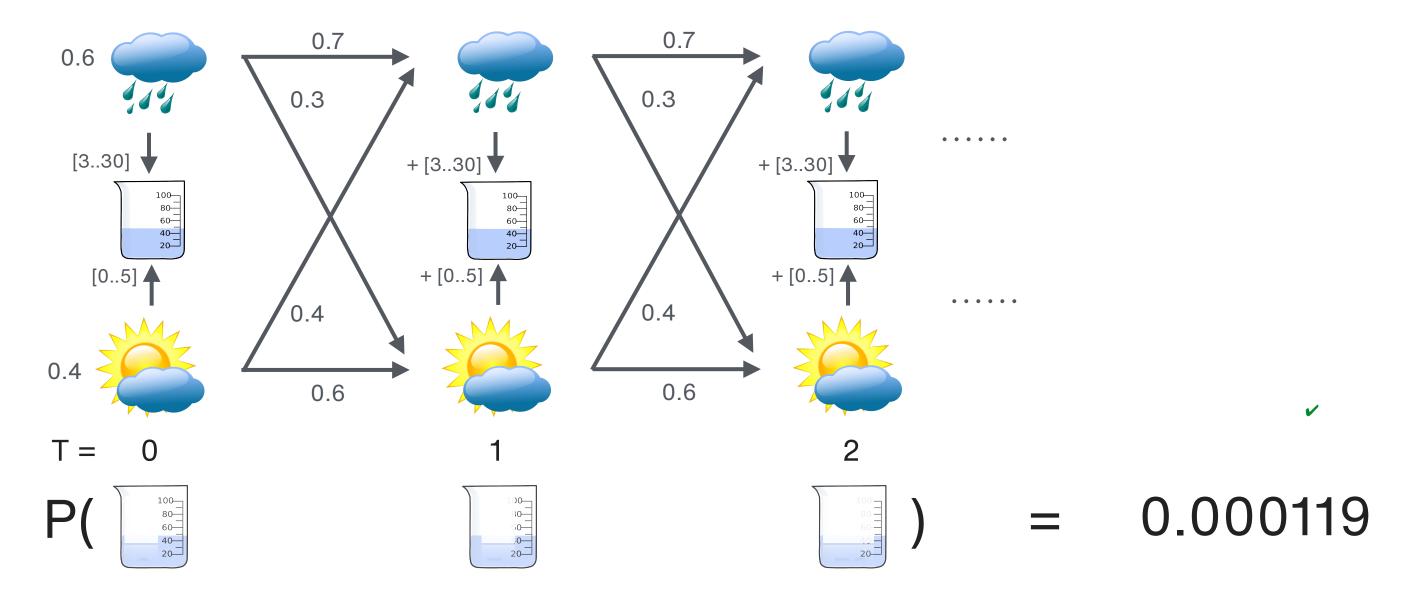
Top-down variable elimination with caching of results

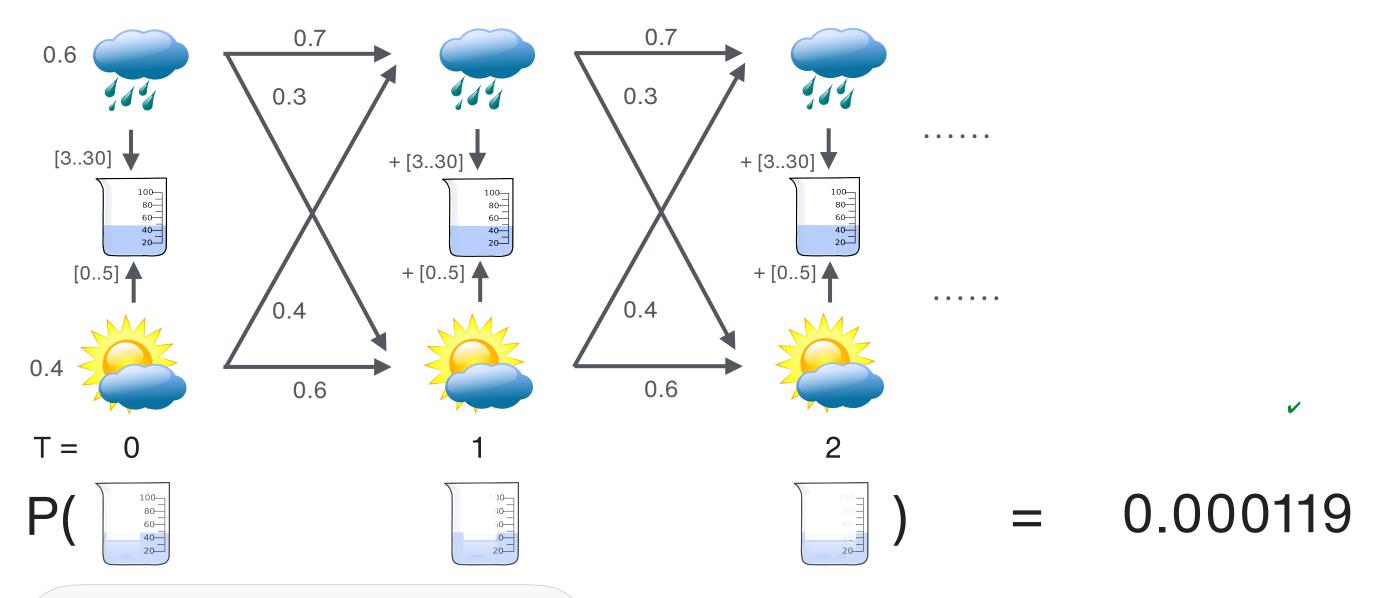
Strong Python integration



Contribution:

"Inconsistency Pruning" for better efficiency



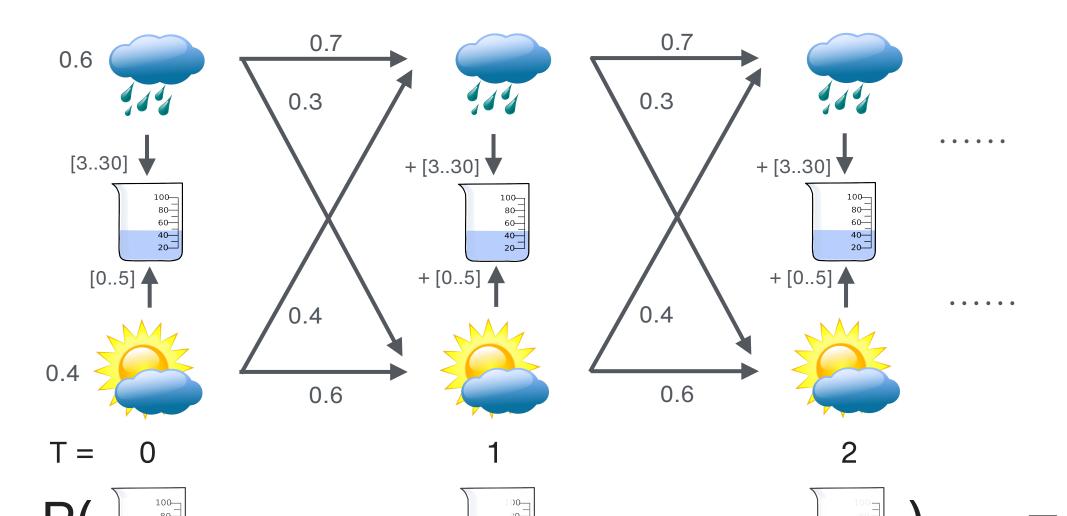


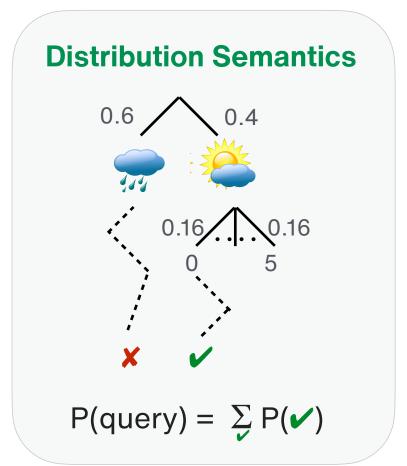
state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

state ~ [[rainy, 0.7], [sunny, 0.3]] @ T+1 :- state=rainy @ T.

obs ~ [R+3..R+30] @ T :state=rainy @ T, T > 0, obs=R @ T-1.

?- obs=0 @ 0, obs=4 @ 1, obs=20 @ 2.





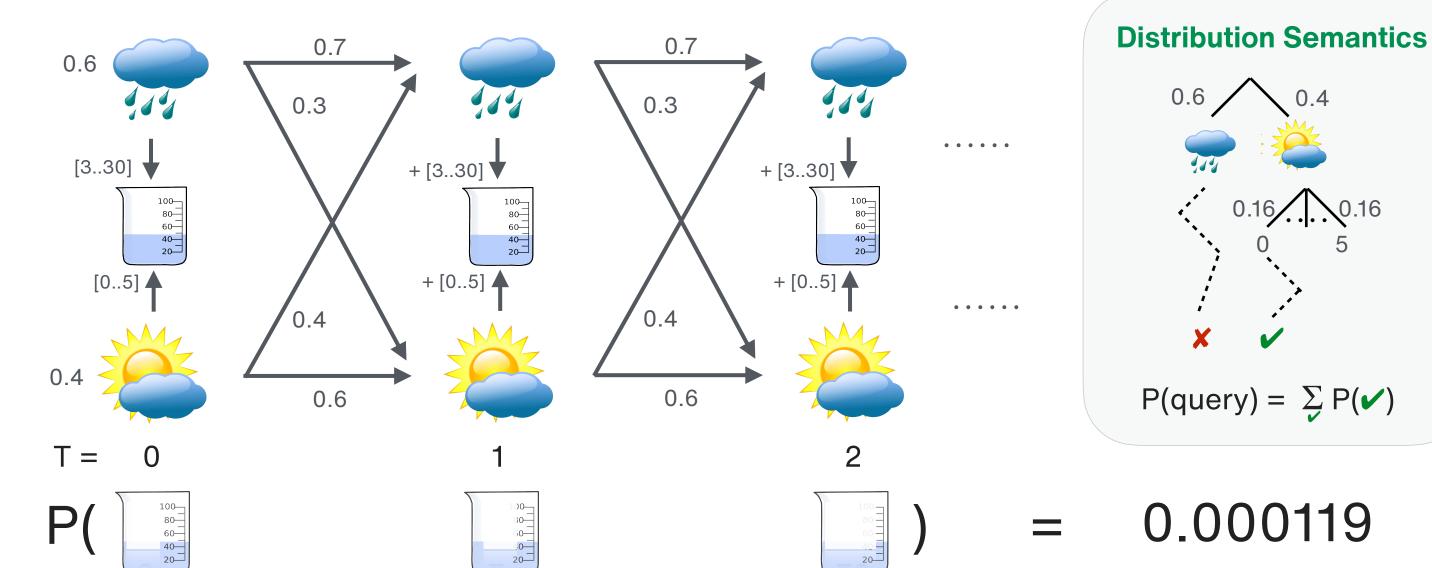
0.000119

state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

state ~ [[rainy, 0.7], [sunny, 0.3]] @ T+1 :- state=rainy @ T.

obs ~ [R+3..R+30] @ T :state=rainy @ T, T > 0, obs=R @ T-1.

?- obs=0 @ 0, obs=4 @ 1, obs=20 @ 2.



state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

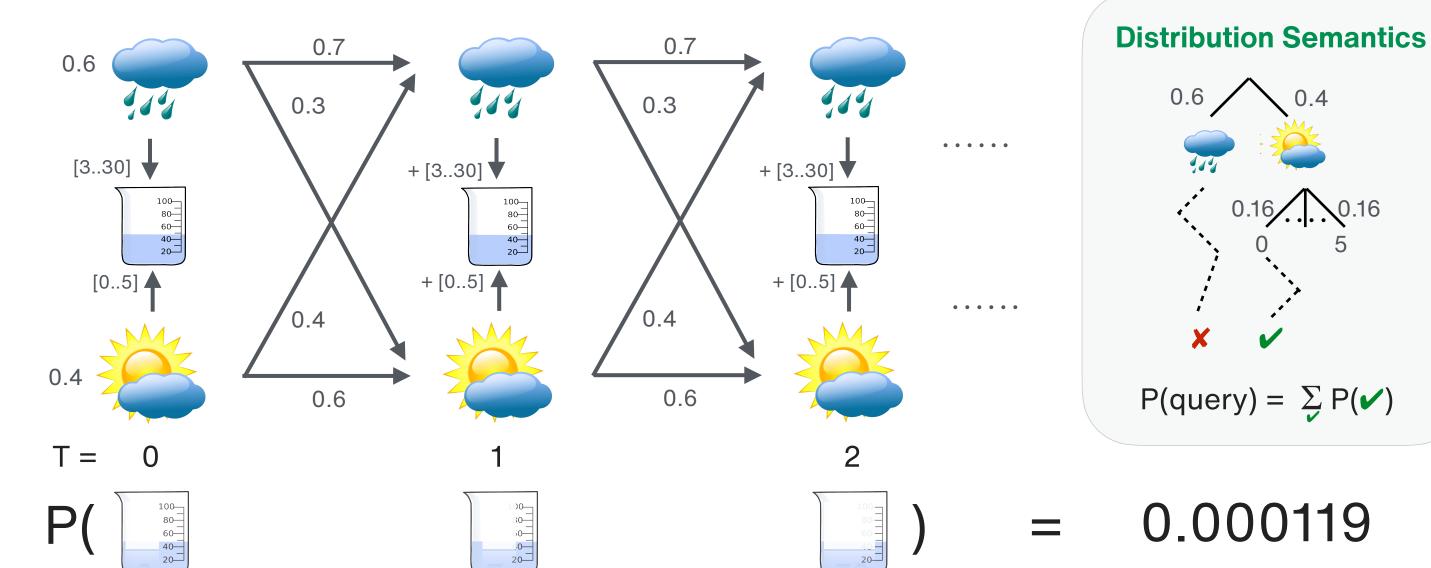
state ~ [[rainy, 0.7], [sunny, 0.3]] @ T+1 :- state=rainy @ T.

obs ~ [R+3..R+30] @ T :state=rainy @ T, T > 0, obs=R @ T-1.

?- obs=0 @ 0, obs=4 @ 1, obs=20 @ 2.

Computing query success probabilities

- (1) Program grounding (≈ Bayes net)
- (2) Query probability (marginal probability by var. elim.)



state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

state ~ [[rainy, 0.7], [sunny, 0.3]] @ T+1 :- state=rainy @ T.

obs ~ [R+3..R+30] @ T :state=rainy @ T, T > 0, obs=R @ T-1.

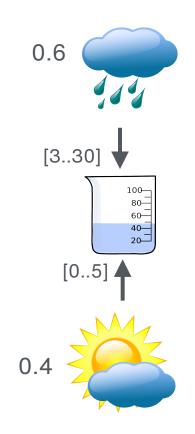
?- obs=0 @ 0, obs=4 @ 1, obs=20 @ 2.

Computing query success probabilities

- (1) Program grounding (≈ Bayes net)
- (2) Query probability (marginal probability by var. elim.)

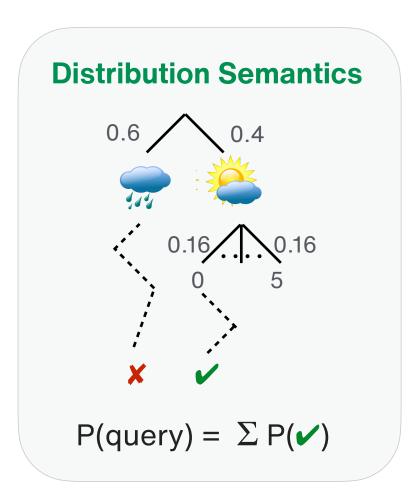
Naive (1): too many rules (quadratic in this case)

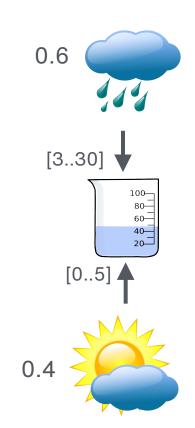
Solution: "Inconsistency Pruning"



(Already grounded) program rules T = 0

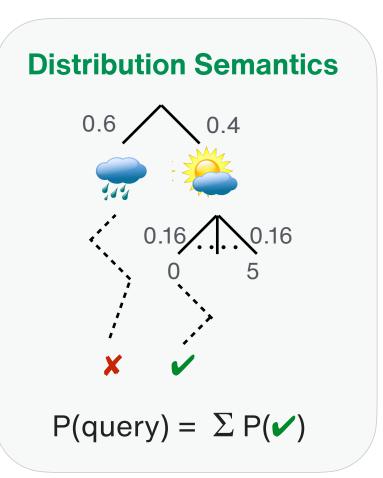
state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.
obs ~ [3..30] @ 0 :- state=rainy @ 0.
obs ~ [0..5] @ 0 :- state=sunny @ 0.





In increasing time order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- _ Extend current domain with \ \ \ \ heads

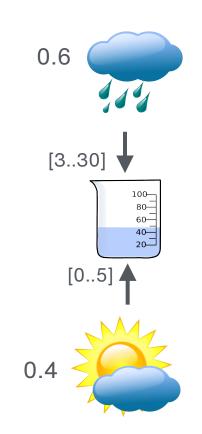


(Already grounded) program rules T = 0

state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

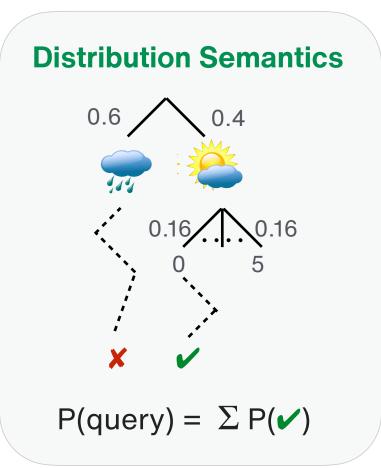
obs ~ [3..30] @ 0 :- state=rainy @ 0.

obs ~ [0..5] @ 0 :- state=sunny @ 0.



In increasing time order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- _ Extend current domain with | heads



(Already grounded) program rules T = 0

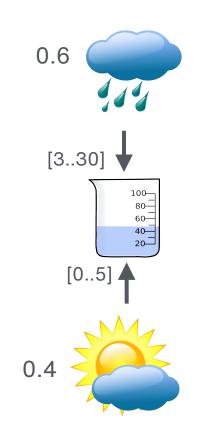
state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

obs ~ [3..30] @ 0 :- state=rainy @ 0.

obs ~ [0..5] @ 0 :- state=sunny @ 0.

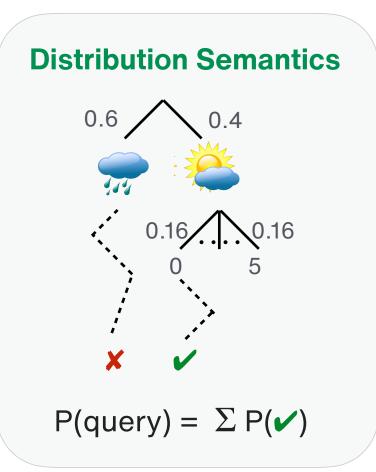
Strengthen query by regression





In increasing time order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- _ Extend current domain with \ \ \ \ heads



(Already grounded) program rules T = 0

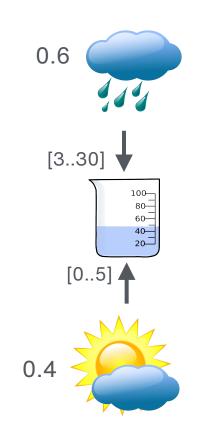
state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

obs ~ [3..30] @ 0 :- state=rainy @ 0.

obs ~ [0..5] @ 0 :- state=sunny @ 0.

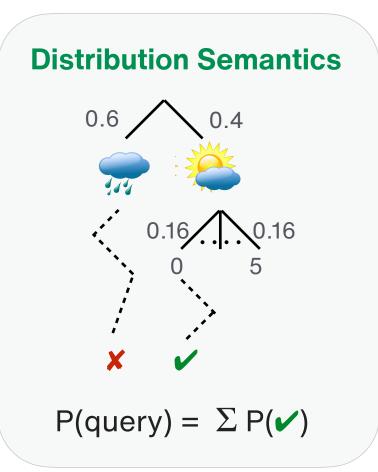
Strengthen query by regression





In increasing time order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- _ Extend current domain with | heads



(Already grounded) program rules T = 0

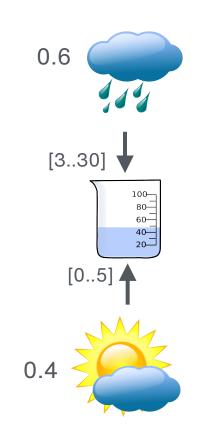
state ~ [[rainy, 0.6], [sunny, 0.4]] @ 0.

obs ~ [3..30] @ 0 :- state=rainy @ 0.

obs ~ [0..5] @ 0 :- state=sunny @ 0.

Strengthen query by regression





In increasing time order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- _ Extend current domain with \ \ \ heads

Distribution Semantics $0.6 \qquad 0.4$ $0.16 \qquad 0.16$ $0 \qquad 5$ P(query) = $\Sigma P(\checkmark)$

(Already grounded) program rules T = 0



obs [3..30] @ Or state rainy @ Or IP pruning

obs ~ [0..5] @ 0 :- state=sunny @ 0.



Domain after T = 0

state = rainy @ 0.

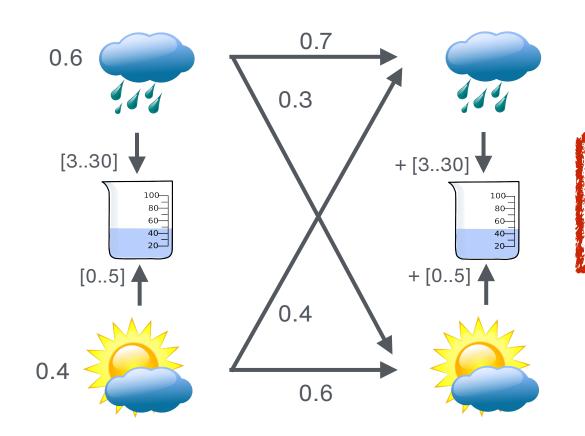
state = sunny @ 0.

obs = 0 @ 0.

obs = 1 @ 0.

•

obs = 5 @ 0.



In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- Extend current domain with heads

Distribution Semantics 0.6 0.4 0.16 0.16 5

$$P(query) = \sum P(\checkmark)$$

Domain T = 1

obs =
$$0 @ 0$$
.

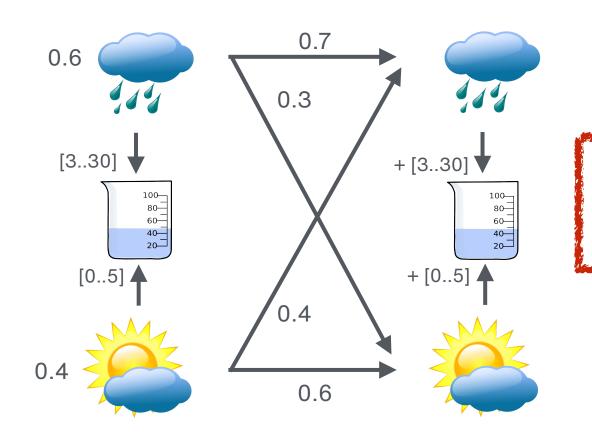
obs =
$$1 @ 0$$
.

obs =
$$5 @ 0$$
.

state = rainy @
$$1$$
.

state = sunny @
$$1$$
.

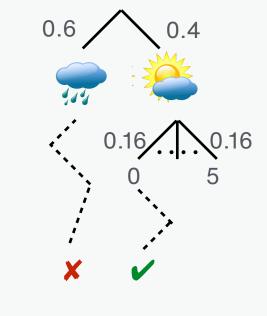
obs ~ [R+3..R+30] @ T :state=rainy @ T, T > 0, obs=R @ T-1.



In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- Extend current domain with \times heads

Distribution Semantics



$P(query) = \sum P(\checkmark)$

Domain T = 1



obs =
$$0 @ 0$$
.

obs =
$$1 @ 0$$
.

:

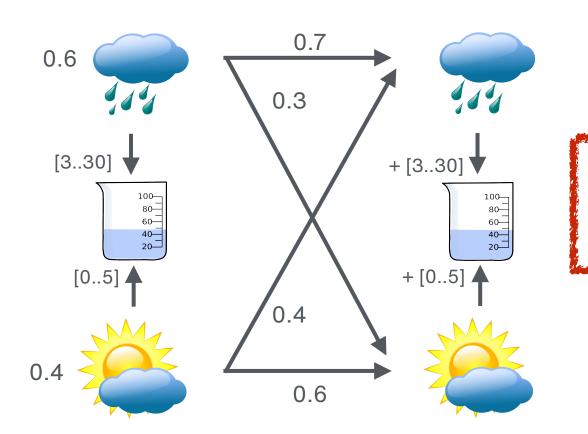
obs =
$$5 @ 0$$
.

state = sunny @ 1.

Grounded program rules T = 1

•

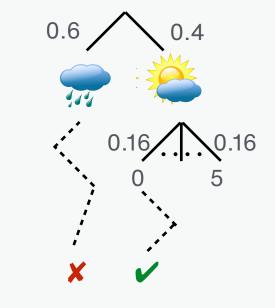
:



In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
 - Extend current domain with beads

Distribution Semantics



$$P(query) = \sum P(\checkmark)$$

Domain T = 1



obs =
$$0 @ 0$$
.

obs =
$$1 @ 0$$
.

:

obs =
$$5 @ 0$$
.

state = rainy @ 1.

state = sunny @ 1.

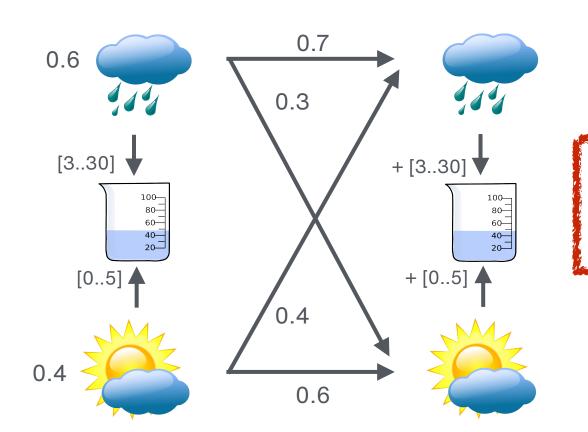
Grounded program rules T = 1

:

obs
$$\sim [0..5]$$
 @ 1:- state=sunny @ 1, obs=0 @ 0.

obs ~
$$[1..6]$$
 @ 1 :- state=sunny @ 1, obs=1 @ 0.

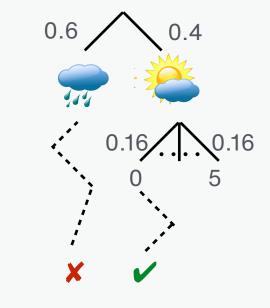
:



In increasing stratification order:

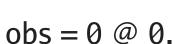
- Ground out program over current domain
- Query regression, inconsistency pruning
 - Extend current domain with \ \ \ \ heads

Distribution Semantics



$$P(query) = \sum P(\checkmark)$$

Domain T = 1



obs = 1 @ 0.

:

obs = 5 @ 0.

state = rainy @ 1.

state = sunny @ 1.

Grounded program rules T = 1

obs ~ [3..30] @ 1 :- state=rainy @ 1, obs=0 @ 0.

obs ~ [4..31] @ 1 :- state=rainy @ 1, obs=1 @ 0.

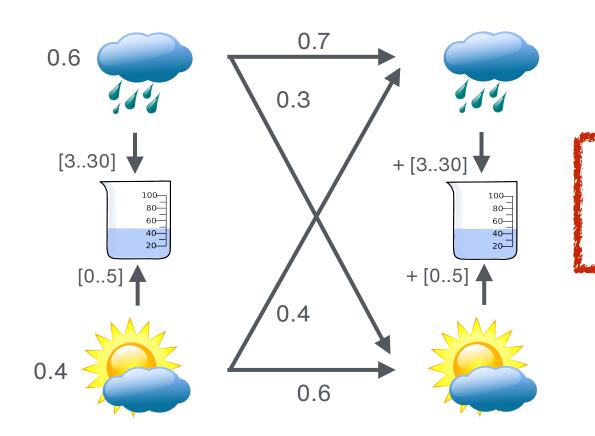
:

obs ~ [0..5] @ 1 :- state=sunny @ 1, obs=0 @ 0.

obs ~ [1..6] @ 1 :- state=sunny @ 1, obs=1 @ 0.

:

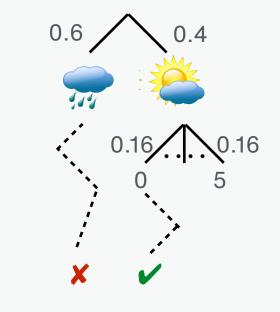
obs ~ [R+3..R+30] @ T :state=rainy @ T,
T > 0,
obs=R @ T-1.



In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- Extend current domain with \ \ \ \ heads

Distribution Semantics



$$P(query) = \sum P(\checkmark)$$

Domain T = 1



obs = 0 @ 0.

obs = 1 @ 0.

:

obs = 5 @ 0.

state = rainy @ 1.

state = sunny @ 1.

Grounded program rules T = 1

obs ~ [3..30] @ 1 :- state=rainy @ 1, obs=0 @ 0.

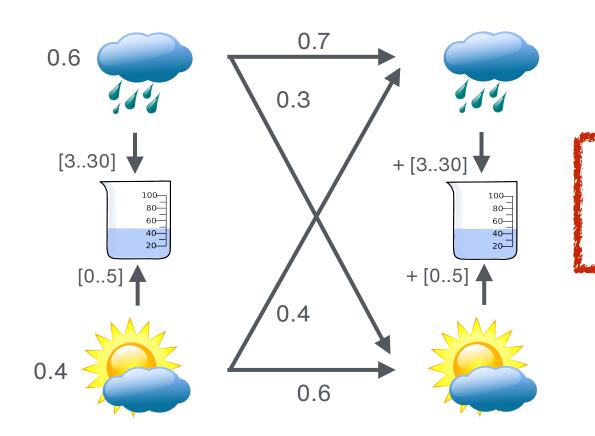
obs ~ [4..31] @ 1 :- state=rainy @ 1; obs=1 @ 0.

obs ~ [0..5] @ 1 :- state=sunny @ 1, obs=0 @ 0.

obs ~ [1..6] @ 1:- state=sunny @ 1; obs=1 @ 0

17

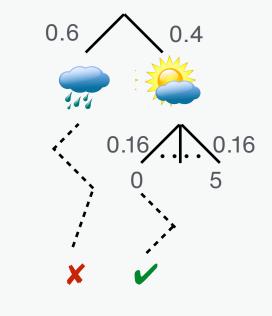
obs ~ [R+3..R+30] @ T :state=rainy @ T,
T > 0,
obs=R @ T-1.



In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- Extend current domain with \ \ \ \ heads

Distribution Semantics



$$P(query) = \sum P(\checkmark)$$

Domain T = 1



obs = 1 @ 0.

:

obs = 5 @ 0.

state = rainy @ 1.

state = sunny @ 1.

Grounded program rules T = 1

obs ~ [3..30] @ 1 :- state=rainy @ 1, obs=0 @ 0.

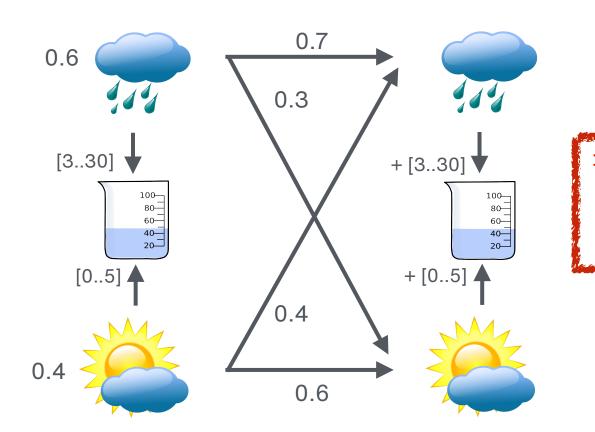
obs ~ [4..31] @ 1:- state=rainy @ 1; ubs=1 @ 0.

obs ~ [0..5] @ 1 :- state=sunny @ 1, obs=0 @ 0.

obs ~ [1..6] @ 1 :- state=sunny @ 1, obs=1 @ 0

obs ~ [R+3..R+30] @ T :state=rainy @ T,
T > 0,
obs=R @ T-1.

Inconsistency pruning: 62 -> 2 rules

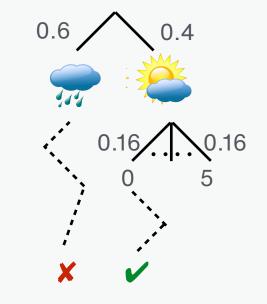


In increasing stratification order:

- Ground out program over current domain
- Query regression, inconsistency pruning
- Extend current domain with \ \ \ heads

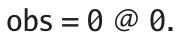


Distribution Semantics



$$P(query) = \sum P(\checkmark)$$

Domain T = 1



obs = 1 @ 0.

:

obs = 5 @ 0.

state = rainy @ 1.

state = sunny @ 1.

Grounded program rules T = 1

obs ~ [3..30] @ 1 :- state=rainy @ 1, obs=0 @ 0.

obs ~ [4..31] @ 1 :- state=rainy @ 1; obs=1 @ 0.

obs ~ [0..5] @ 1 :- state=sunny @ 1, obs=0 @ 0.

obs ~ [1..6] @ 1:- state=sunny @ 1; obs=1 @ 0

obs ~ [R+3..R+30] @ T :state=rainy @ T,
T > 0,
obs=R @ T-1.

Inconsistency pruning: 62 -> 2 rules

Experimental Evaluation 1 - Hidden Markov Model

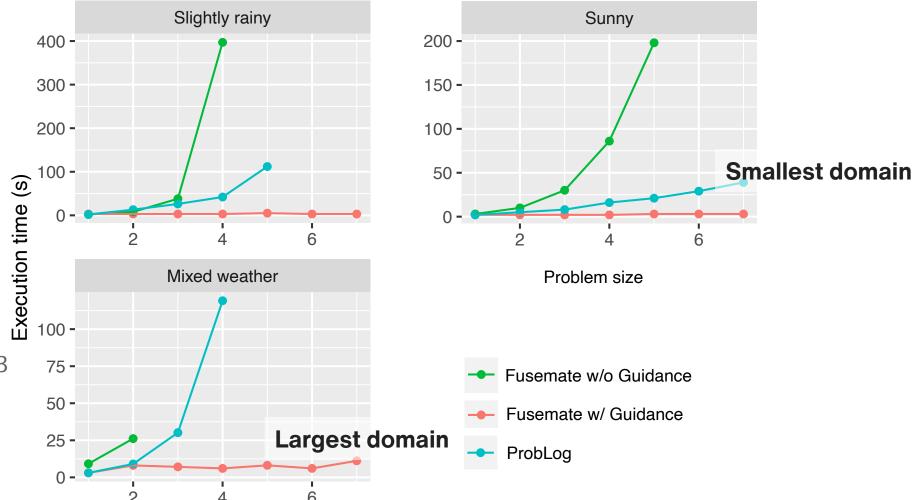
Runtime Results Fusemate vs ProbLog

Rainy/sunny example from above

```
%% Queries for N=3
%% Sunny
?-state=X @ 3 | obs=0 @ 1, obs=0 @ 2, obs=0 @ 3.

%% Rainy
?-state=X @ 3 | obs=4 @ 1, obs=8 @ 2, obs=12 @ 3

%% Mixed
state=X @ 3 | obs=0 @ 1, obs=4 @ 2, obs=24 @ 3.
```



Experimental Evaluation 1 - Hidden Markov Model

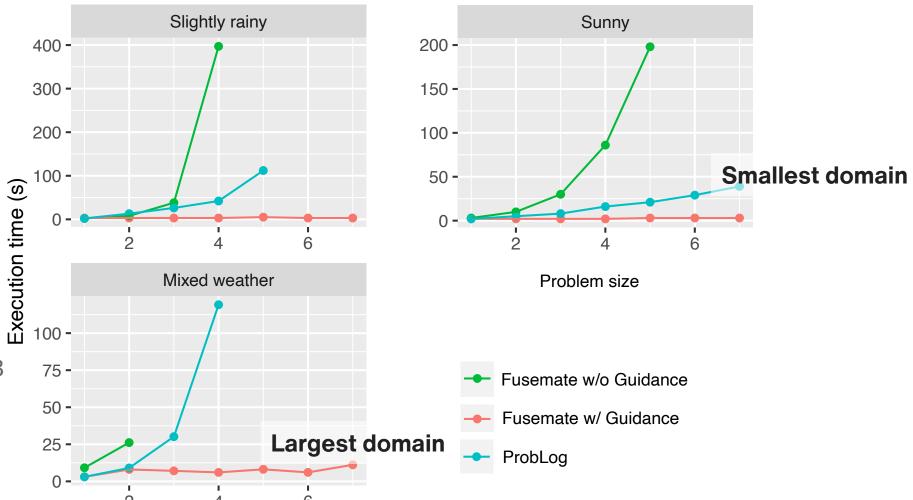
Runtime Results Fusemate vs ProbLog

Rainy/sunny example from above

```
%% Queries for N=3
%% Sunny
?-state=X @ 3 | obs=0 @ 1, obs=0 @ 2, obs=0 @ 3.

%% Rainy
?-state=X @ 3 | obs=4 @ 1, obs=8 @ 2, obs=12 @ 3

%% Mixed
state=X @ 3 | obs=0 @ 1, obs=4 @ 2, obs=24 @ 3.
```



Grounding vs Inference - Mixed Weather

	Fusemate #gre	ound rules	Pro	obLog	
N	query-guided	unguided	total time	grounding time	#ground rules
2	2200	6500	9.0	8.3	53
3	2270	12900	30	19	276
4	2300	21400	119	33	499
5	2400	32000		50	682
6	2470	45000		65	839
_ 7	2500	60000		95	1068

Experimental Evaluation 1 - Hidden Markov Model

Runtime Results Fusemate vs ProbLog

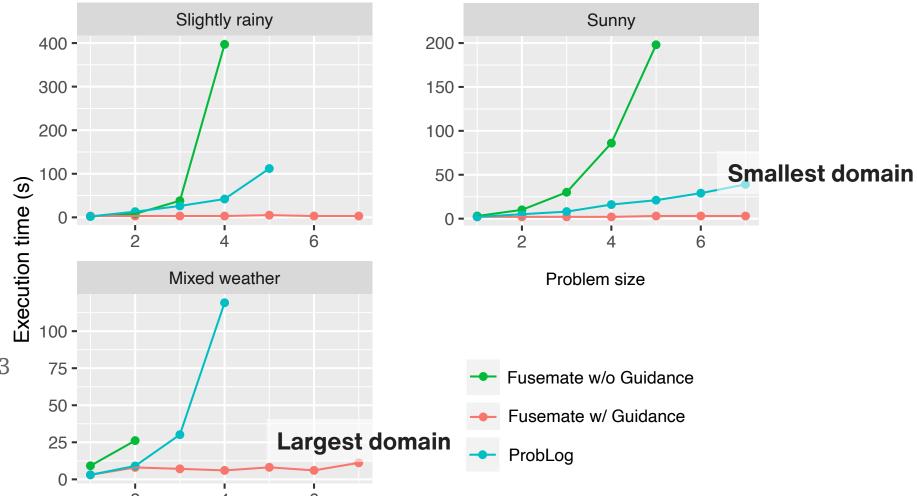
Rainy/sunny example from above

```
%% Queries for N=3
%% Sunny
?-state=X @ 3 | obs=0 @ 1, obs=0 @ 2, obs=0 @ 3.

%% Rainy
?-state=X @ 3 | obs=4 @ 1, obs=8 @ 2, obs=12 @ 3
```

%% Mixed

state=X @ 3 | obs=0 @ 1, obs=4 @ 2, obs=24 @ 3.



Grounding vs Inference - Mixed Weather

	Fusemate #gr	ound rules	Pro	obLog	
N	query-guided	unguided	total time	grounding time	#ground rules
2	2200	6500	9.0	8.3	53
3	2270	12900	30	19	276
4	2300	21400	119	33	499
5	2400	32000		50	682
6	2470	45000		65	839
7	2500	60000		95	1068

Fusemate:

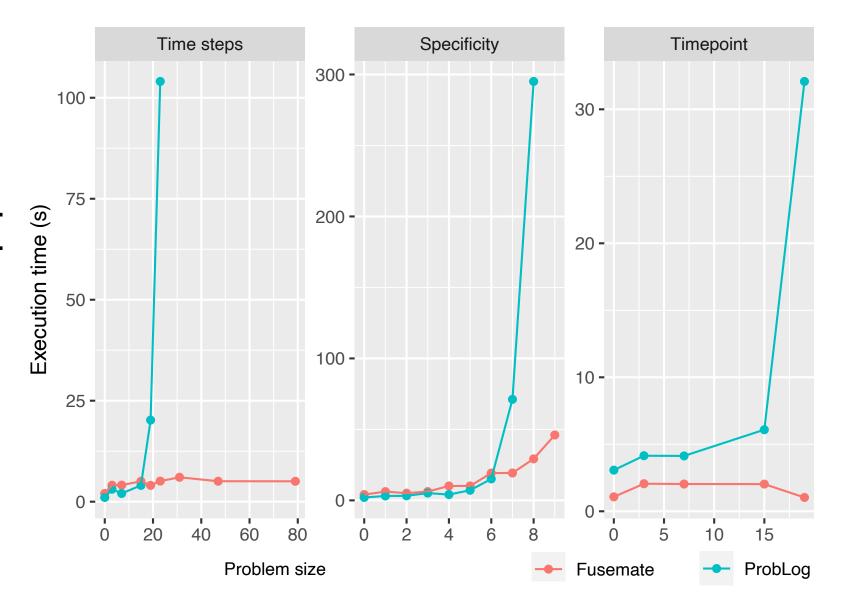
Improved grounding pays off
Inference engine implements UNA
ProbLog:

Grounding OK?

Bottleneck inference component?

Experimental Evaluation 2 - Markov Model

Runtime Results Fusemate vs ProbLog



(ProbLog code from ProbLog tutorial web page)

Probability parameters learning

MLE, EM

Learning the structure of logic programs

Inductive Logic Programming (1970s)

Probabilistic Version [Riguzzi 2015]

Logic programs from tabular data

Probabilistic version of CART

Probabilistic decision lists [2017]

FOLD-RM [Gupta et al, ICLP 2023]

CON-FOLD [McGinness and B, ICLP 2024]

= FOLD-RM with confidence values

Very short explanations



	Passengerld	Survived	Pclass	Title	Sex	Age	SibSp	Parch	
0	1	False	3	Mr	male	22	1	0	
1	2	True	1	Mrs	female	38	1	0	
2	3	True	3	Miss	female	26	0	0	STON/0
3	4	True	1	Mrs	female	35	1	0	
4	5	False	3	Mr	male	NaN	0	0	

```
survived(X) := not perished(X).
```

perished(X) := not sex(X, female).

perished(X) :-

sex(X, female), pclass(X, 3),

fare(X, N), not N \leq 23.25.

Probability parameters learning

MLE, EM

Learning the structure of logic programs

Inductive Logic Programming (1970s)

Probabilistic Version [Riguzzi 2015]

Logic programs from tabular data

Probabilistic version of CART

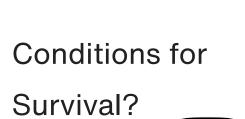
Probabilistic decision lists [2017]

FOLD-RM [Gupta et al, ICLP 2023]

CON-FOLD [McGinness and B, ICLP 2024]

= FOLD-RM with confidence values

Very short explanations





	Passengerld	Survived	Pclass	Title	Sex	Age	SibSp	Parch	
0	1	False	3	Mr	male	22	1	0	
1	2	True	1	Mrs	female	38	1	0	
2	3	True	3	Miss	female	26	0	0	STON/C
3	4	True	1	Mrs	female	35	1	0	
4	5	False	3	Mr	male	NaN	0	0	

```
survived(X) := not perished(X).
```

perished(X) := not sex(X, female).

perished(X) :-

sex(X, female), pclass(X, 3),

fare(X, N), not N \leq 23.25.

Probability parameters learning

MLE, EM

Learning the structure of logic programs

Inductive Logic Programming (1970s)

Probabilistic Version [Riguzzi 2015]

Logic programs from tabular data

Probabilistic version of CART

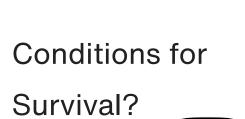
Probabilistic decision lists [2017]

FOLD-RM [Gupta et al, ICLP 2023]

CON-FOLD [McGinness and B, ICLP 2024]

= FOLD-RM with confidence values

Very short explanations





	Passengerld	Survived	Pclass	Title	Sex	Age	SibSp	Parch	
0	1	False	3	Mr	male	22	1	0	
1	2	True	1	Mrs	female	38	1	0	
2	3	True	3	Miss	female	26	0	0	STON/C
3	4	True	1	Mrs	female	35	1	0	
4	5	False	3	Mr	male	NaN	0	0	

```
survived(X) := not perished(X).
```

perished(X) := not sex(X, female).

perished(X) :-

sex(X, female), pclass(X, 3),

fare(X, N), not N \leq 23.25.

Probability parameters learning

MLE, EM

Learning the structure of logic programs

Inductive Logic Programming (1970s)

Probabilistic Version [Riguzzi 2015]

Logic programs from tabular data

Probabilistic version of CART

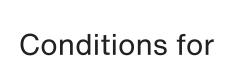
Probabilistic decision lists [2017]

FOLD-RM [Gupta et al, ICLP 2023]

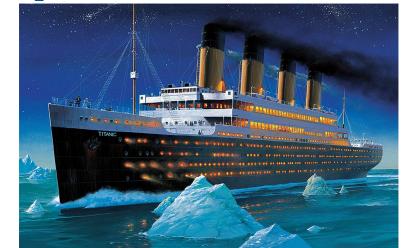
CON-FOLD [McGinness and B, ICLP 2024]

= FOLD-RM with confidence values

Very short explanations



Survival?



	PassengerId	Survived	Pclass	Title	Sex	Age	SibSp	Parch	
0	1	False	3	Mr	male	22	1	0	
1	2	True	1	Mrs	female	38	1	0	
2	3	True	3	Miss	female	26	0	0	STON/0
3	4	True	1	Mrs	female	35	1	0	
4	5	False	3	Mr	male	NaN	0	0	

```
0.97 survived(X) := not perished(X).
    perished(X) := not sex(X, female).
    perished(X) :=
        sex(X, female), pclass(X, 3),
        fare(X, N), not N <= 23.25.</pre>
```

Probability parameters learning

MLE, EM

Learning the structure of logic programs

Inductive Logic Programming (1970s)

Probabilistic Version [Riguzzi 2015]

Logic programs from tabular data

Probabilistic version of CART

Probabilistic decision lists [2017]

FOLD-RM [Gupta et al, ICLP 2023]

CON-FOLD [McGinness and B, ICLP 2024]

= FOLD-RM with confidence values

Very short explanations



Survival?



	Passengerld	Survived	Pclass	Title	Sex	Age	SibSp	Parch	
0	1	False	3	Mr	male	22	1	0	
1	2	True	1	Mrs	female	38	1	0	
2	3	True	3	Miss	female	26	0	0	STON/0
3	4	True	1	Mrs	female	35	1	0	
4	5	False	3	Mr	male	NaN	0	0	

 $\frac{0.97}{0.97}$ survived(X) :- not perished(X).

0.9 perished(X) :- not sex(X, female).

perished(X) :-

sex(X, female), pclass(X, 3),

fare(X, N), not $N \leftarrow 23.25$.

Part 1

- Probabilistic
- Logic
- Programming
- Fusemate Implementation

Part 2

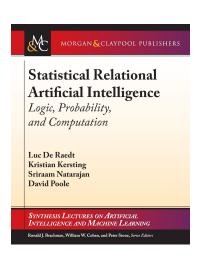
- LLMs + Logic (Programming)
- Neural Networks + Logic (Programming)

StarAI =

RelationalAI/Logic +

Learning + Statistics (1980s)

Fusemate



NeSy =

Neural Networks + Symbolic Reasoning

Neural-Symbolic Learning and Reasoning:
A Survey and Interpretation

Tarek R. Besold et al

TAREK-R.BESOLD@CITY.AC.UK

Department of Computer Science, City, University of London

NeSy + StarAl?

From Statistical Relational to Neural Symbolic Artificial Intelligence: a Survey.

Giuseppe Marra^a, Sebastijan Dumančić^c, Robin Manhaeve^a, Luc De Raedt^{a,b}

^aKU Leuven, Department of Computer Science and Leuven.AI ^bÖrebro University, Center for Applied Autonomous Sensor Systems ^cDelft University of Technology, Department of Software Technology

DeepProbLog - see below

LLMs + Logic

Augmented Language Models: a Survey

Grégoire Mialon* et al

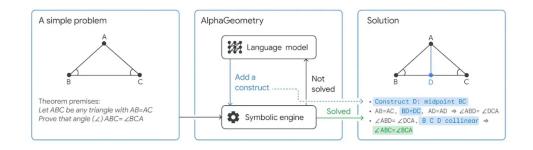
gmialon@meta.com

See below

Position: LLMs Can't Plan, But Can Help Planning in LLM-Modulo Frameworks

Subbarao Kambhampati ¹ Karthik Valmeekam ¹ Lin Guan ¹ Mudit Verma ¹ Kaya Stechly ¹ Siddhant Bhambri ¹ Lucas Saldyt ¹ Anil Murthy ¹

AlphaZero -> AlphaGeometry, AlphaProof

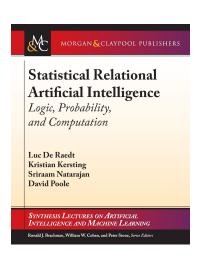


StarAI =

RelationalAI/Logic +

Learning + Statistics (1980s)

Fusemate



NeSy =

Neural Networks + Symbolic Reasoning

Neural-Symbolic Learning and Reasoning:
A Survey and Interpretation

Tarek R. Besold et al

TAREK-R.BESOLD@CITY.AC.UK

Department of Computer Science, City, University of London

NeSy + StarAl?

From Statistical Relational to Neural Symbolic Artificial Intelligence: a Survey.

Giuseppe Marra^a, Sebastijan Dumančić^c, Robin Manhaeve^a, Luc De Raedt^{a,b}

^aKU Leuven, Department of Computer Science and Leuven.AI ^bÖrebro University, Center for Applied Autonomous Sensor Systems ^cDelft University of Technology, Department of Software Technology

DeepProbLog - see below

LLMs + Logic

Augmented Language Models: a Survey

Grégoire Mialon* et al

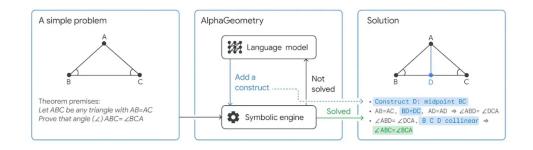
gmialon@meta.com

See below

Position: LLMs Can't Plan, But Can Help Planning in LLM-Modulo Frameworks

Subbarao Kambhampati ¹ Karthik Valmeekam ¹ Lin Guan ¹ Mudit Verma ¹ Kaya Stechly ¹ Siddhant Bhambri ¹ Lucas Saldyt ¹ Anil Murthy ¹

AlphaZero -> AlphaGeometry, AlphaProof

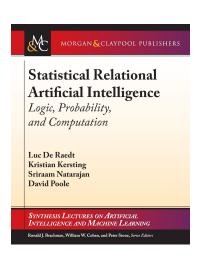


StarAI =

RelationalAI/Logic +

Learning + Statistics (1980s)

Fusemate



NeSy =

Neural Networks + Symbolic Reasoning

Neural-Symbolic Learning and Reasoning:
A Survey and Interpretation

Tarek R. Besold et al

TAREK-R.BESOLD@CITY.AC.UK

Department of Computer Science, City, University of London

NeSy + StarAl?

From Statistical Relational to Neural Symbolic Artificial Intelligence: a Survey.

Giuseppe Marra^a, Sebastijan Dumančić^c, Robin Manhaeve^a, Luc De Raedt^{a,b}

^aKU Leuven, Department of Computer Science and Leuven.AI ^bÖrebro University, Center for Applied Autonomous Sensor Systems ^cDelft University of Technology, Department of Software Technology

DeepProbLog - see below

LLMs + Logic

Augmented Language Models: a Survey

Grégoire Mialon* et al

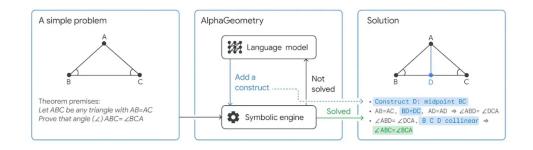
gmialon@meta.com

See below

Position: LLMs Can't Plan, But Can Help Planning in LLM-Modulo Frameworks

Subbarao Kambhampati ¹ Karthik Valmeekam ¹ Lin Guan ¹ Mudit Verma ¹ Kaya Stechly ¹ Siddhant Bhambri ¹ Lucas Saldyt ¹ Anil Murthy ¹

AlphaZero -> AlphaGeometry, AlphaProof

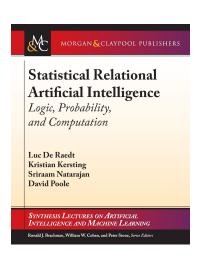


StarAI =

RelationalAI/Logic +

Learning + Statistics (1980s)

Fusemate



NeSy =

Neural Networks + Symbolic Reasoning

Neural-Symbolic Learning and Reasoning:
A Survey and Interpretation

Tarek R. Besold et al

TAREK-R.BESOLD@CITY.AC.UK

Department of Computer Science, City, University of London

NeSy + StarAl?

From Statistical Relational to Neural Symbolic Artificial Intelligence: a Survey.

Giuseppe Marra^a, Sebastijan Dumančić^c, Robin Manhaeve^a, Luc De Raedt^{a,b}

^aKU Leuven, Department of Computer Science and Leuven.AI ^bÖrebro University, Center for Applied Autonomous Sensor Systems ^cDelft University of Technology, Department of Software Technology

DeepProbLog - see below

LLMs + Logic

Augmented Language Models: a Survey

Grégoire Mialon* et al

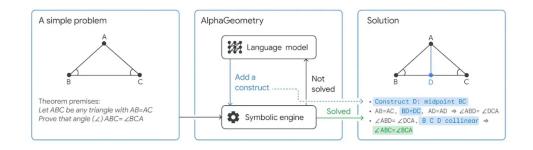
gmialon@meta.com

See below

Position: LLMs Can't Plan, But Can Help Planning in LLM-Modulo Frameworks

Subbarao Kambhampati ¹ Karthik Valmeekam ¹ Lin Guan ¹ Mudit Verma ¹ Kaya Stechly ¹ Siddhant Bhambri ¹ Lucas Saldyt ¹ Anil Murthy ¹

AlphaZero -> AlphaGeometry, AlphaProof

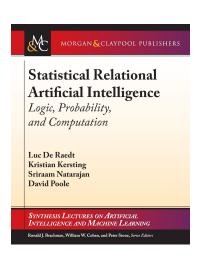


StarAI =

RelationalAI/Logic +

Learning + Statistics (1980s)

Fusemate



NeSy =

Neural Networks + Symbolic Reasoning

Neural-Symbolic Learning and Reasoning:
A Survey and Interpretation

Tarek R. Besold et al

TAREK-R.BESOLD@CITY.AC.UK

Department of Computer Science, City, University of London

NeSy + StarAl?

From Statistical Relational to Neural Symbolic Artificial Intelligence: a Survey.

Giuseppe Marra^a, Sebastijan Dumančić^c, Robin Manhaeve^a, Luc De Raedt^{a,b}

^aKU Leuven, Department of Computer Science and Leuven.AI ^bÖrebro University, Center for Applied Autonomous Sensor Systems ^cDelft University of Technology, Department of Software Technology

DeepProbLog - see below

LLMs + Logic

Augmented Language Models: a Survey

Grégoire Mialon* et al

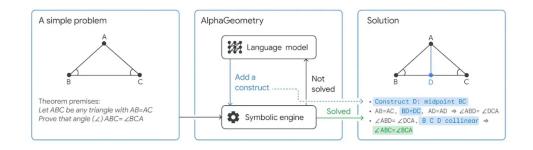
gmialon@meta.com

See below

Position: LLMs Can't Plan, But Can Help Planning in LLM-Modulo Frameworks

Subbarao Kambhampati ¹ Karthik Valmeekam ¹ Lin Guan ¹ Mudit Verma ¹ Kaya Stechly ¹ Siddhant Bhambri ¹ Lucas Saldyt ¹ Anil Murthy ¹

AlphaZero -> AlphaGeometry, AlphaProof



LLM + Logic: LLMs *Are* Logic Reasoners?

Task LLM with Reasoning

ProntoQa [Saparov and He, 2023]

Synthetic Data

Varying redundancy (distractors)

Varying length of reasoning chains

Each composite number is not liquid. Every composite number is a fraction. Every composite number is a number. Negative numbers are not large. Every fraction is large. Each fraction is a real number. Fractions are integers. Integers are temperate. Each number is slow. Each even number is loud. Even numbers are natural numbers. Alex is an even number. Alex is a composite number.

True or false: Alex is large.

Prompt Engineering

In-prompt training one/view shot
Chain-of-thought "explain your reasoning"
Instruct LLM to use strategies
(backward/forward/SOS - own work)
Self-critique

Explainability?

LLM explanation can be nonsense

Correctness and Scalability?

More complex logic, e.g. quantifiers

Planning task, see Subbarao Kambhampati

Reasoning at all?

Or lookup?

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                   gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w(world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property (heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity. Negative numbers are brown. Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                   gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w(world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property(heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                   gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w(world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property(heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                   gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w(world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property(heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                   gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w(world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property(heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                   qminus(friction, speed).
qplus(speed, distance).
                                    gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                   negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w (world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                       property(heat).
                                          property (speed).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

Translation errors?

Reliable Natural Language Understanding with Large Language
Models and Answer Set Programming [Rajasekharan et al, ICLP 2023]

Example 3.1:

```
Question: Alan noticed that his toy car rolls further on a wood floor than on a thick carpet. This suggests that:

(world1: wood floor, world2: thick carpet)

(A) The carpet has more resistance (Solution)

(B) The floor has more resistance
```

Approach LLMs as intelligent parsers

- (1) LLM w/ fine tuning translates problem into logic programming query
- (2) Logic programming system answers query modulo background knowledge

```
gplus(friction, heat).
                                    qminus(friction, speed).
qplus(speed, distance).
                                    gminus (distance, loudness).
positive(X, Y) :- qplus(X, Y).
                                    negative (X, Y) := qminus(X, Y).
positive (X, Y) := qplus(Y, X).
                                   negative (X, Y) := qminus(Y, X).
opposite_w (world1, world2).
                                  opposite_v(higher, lower).
opposite_w(world2,world1).
                                  opposite_v(lower, higher).
conc(P, V, W) :- obs(P, Vr, Wr), property(P),
                 opposite_w(W,Wr), opposite_v(V,Vr).
property (friction).
                                          property (speed).
                       property (heat).
```

Autocorrecting Translation Errors

Automated Theorem Provers Help Improve
Large Language Model Reasoning
[McGinness, B., LPAR 2024]

Each integer is not fruity.
Negative numbers are brown.
Wren is an integer.

LLM (wrong):

```
! [X] : (fruity(X) => integer(X)))
integer(wren)
! [X] : integer(X)
brown(negative)
```

```
! [X] : (fruity(X) => ~ integer(X))
integer(wren)
% ! [X] : integer(X) is an NonFixableError
! [I] : (negative_number(I) => brown(I))
```

DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

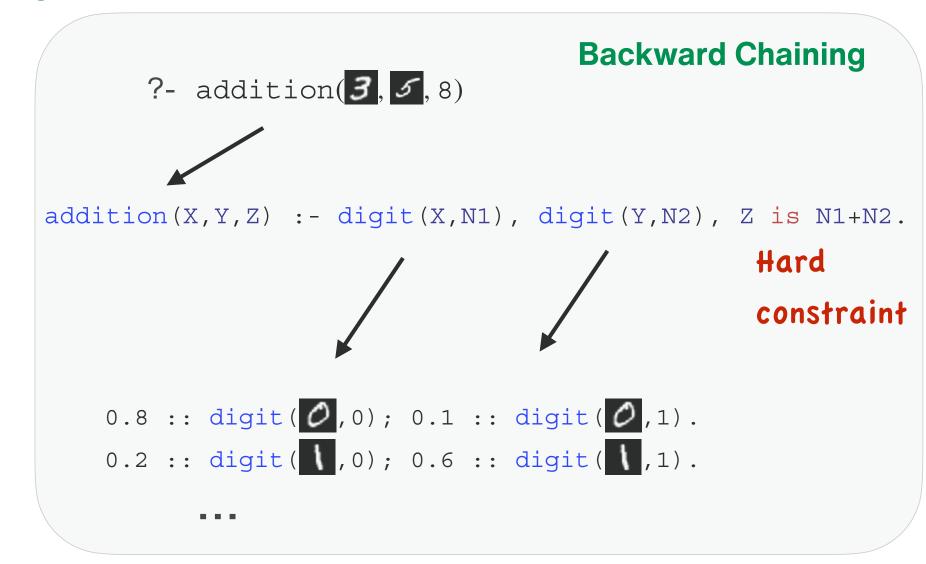
NN classifier for probabilistic facts

Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge



DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

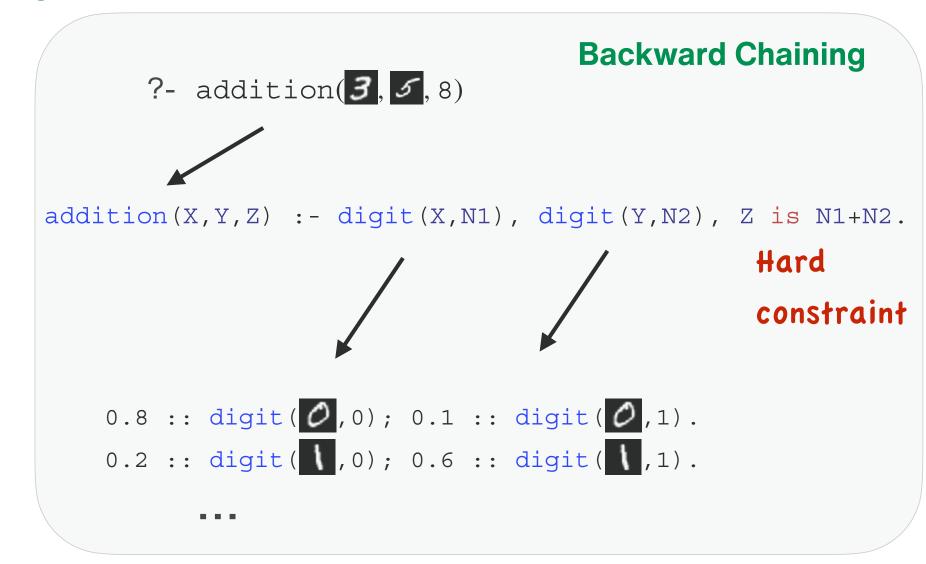
NN classifier for probabilistic facts

Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge



DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

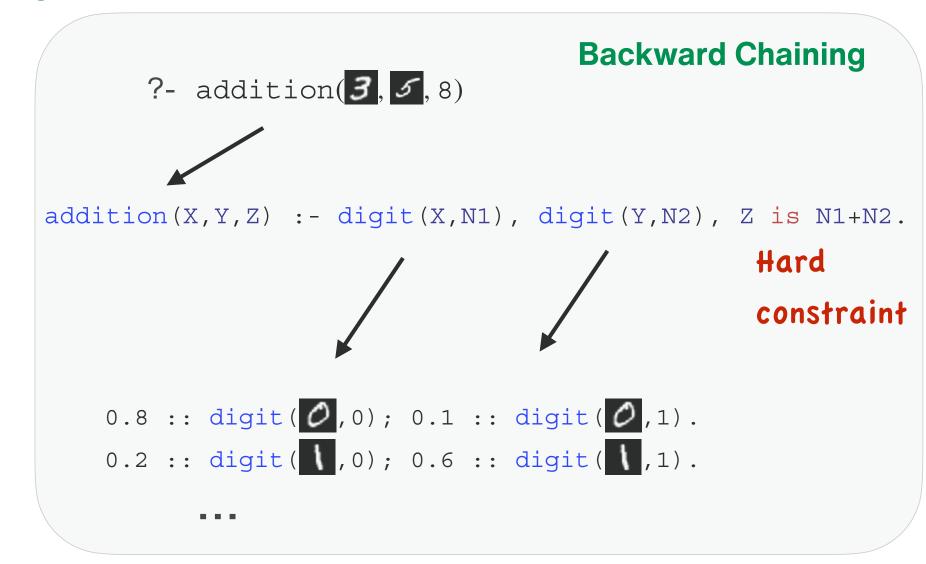
NN classifier for probabilistic facts

Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge



DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

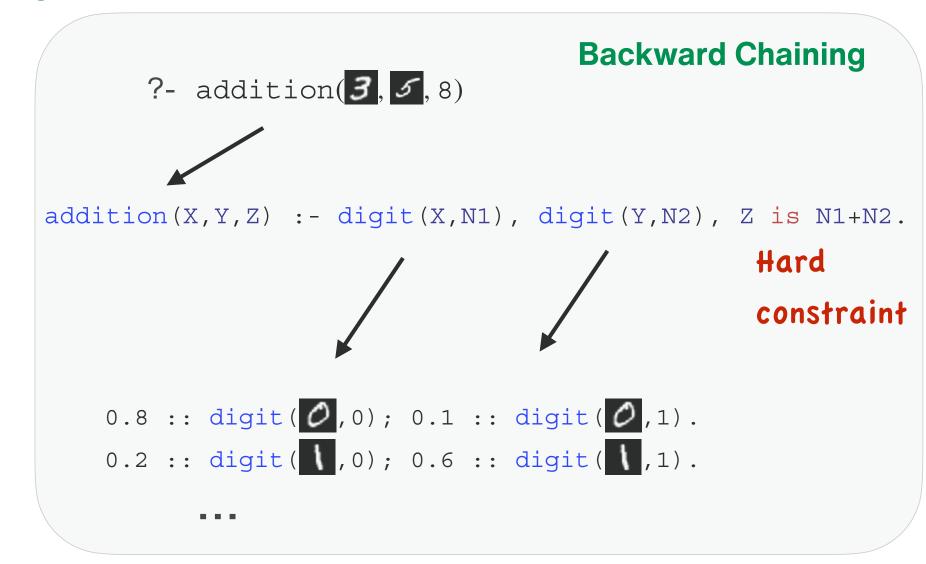
NN classifier for probabilistic facts

Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge



DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

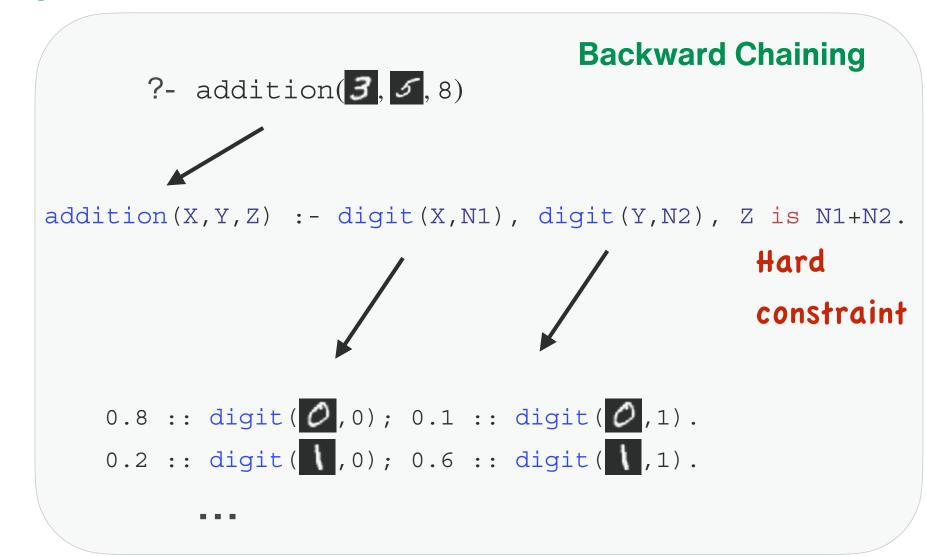
NN classifier for probabilistic facts

Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge



DeepProbLog

Neural probabilistic logic programming in DeepProbLog [Manhaeve et al, AlJ, 2021]

Inference

Query - does the following hold true?

Use backward chaining with

NN classifier for probabilistic facts

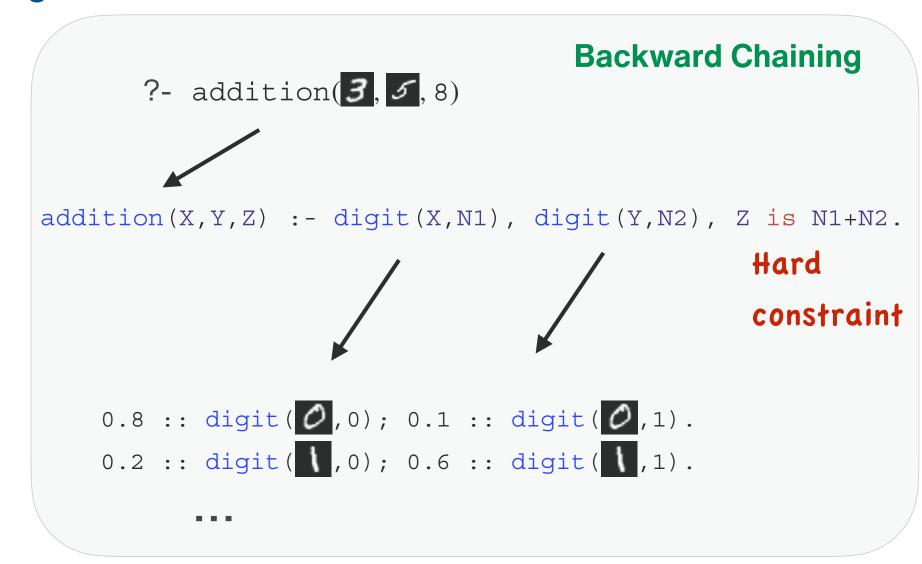
Returns query probability

Learning

End-to-end differentiable

-> back propagation modulo background knowledge

Here: learns digit image classifier from addition examples



"Strong" coupling
Counterpart LLM modulo?

Many More Architectures

- Differentiable Theorem Proving [Rocktäschel]

```
\begin{split} & \texttt{parentOf}(\texttt{HOMER}, \texttt{BART}). \\ & \texttt{grandfatherOf}(X, Y) := \texttt{fatherOf}(X, Z), \texttt{parentOf}(Z, Y). \\ & \texttt{grandfatherOf}(\texttt{ABE}, Q)? \quad \{Q/\texttt{LISA}\}, \{Q/\texttt{BART}\} \end{split}
```

Reasoning in embedding space:

```
Example: unify \mathbf{v}_{\text{grandfather0f}}(\mathbf{X}, \mathbf{v}_{\text{BART}}) with \mathbf{v}_{\text{grandpa0f}}(\mathbf{v}_{\text{ABE}}, \mathbf{v}_{\text{BART}})
\Psi = \{\mathbf{X}/\mathbf{v}_{\text{ABE}}\}, \quad \tau = \min(e^{-\|\mathbf{v}_{\text{grandfather0f}} - \mathbf{v}_{\text{grandpa0f}}\|_2}, e^{-\|\mathbf{v}_{\text{BART}} - \mathbf{v}_{\text{BART}}\|_2})
```

- Semantic Probabilistic Layers for Neuro-Symbolic Learning [Ahmed et al NeurlPS, 2022] Logic constraints at the output layer, e.g. exclusivity constraints for classification
- FFNSL: Feed-Forward Neural-Symbolic Learner [Cunnington, Law, Lobo, Russo 2023]
- Encodings of logic within NNs
- Logic Tensor Networks
- Neural Datalog over time

Conclusions

Fusemate

- Probabilistic Logic Programming system
- Good

Expressivity, good Python interface, reasonably optimized for intended use case (HMM-ish)

- Needs work

Documentation, efficiency

LMM + Logic

- Current focus of research and D61 applications for "Explainability"

ML/LLM -> generate solution candidates

Probabilistic logic -> validate/complete solution candidates